## IIT JEE Formulas

## Maths Formulas

## Part 1

|  | Circle Formula |
| :---: | :---: |
| The formula for circle are as stated below |  |
| Description | Formula |
| Area of a Circle | - In terms of radius: $\pi r^{2}$ <br> - In terms of diameter: $\frac{\pi}{4} \times d^{2}$ |
| Surface Area of a Circle | $\pi r^{2}$ |
| General Equation of a Circle | The general equation of a circle with coordinates of a centre $(h, k)$, and radius $r$ is given as: $\sqrt{(x-h)^{2}+(y-k)^{2}}=r$ |
| Standard Equation of a Circle | The Standard equation of a circle with centre $(a, b)$, and radius $r$ is given as: $(x-a)^{2}+(y-b)^{2}=r^{2}$ |
| Diameter of a Circle | $2 \times$ radius |
| Circumference of a Circle | $2 \pi r$ |
| Intercepts made by Circle | $x^{2}+y^{2}+2 g x+2 f y+c=0$ <br> i. On $x$-axis: $2 \sqrt{g^{2}-c}$ <br> ii. On $y$-axis: $2 \sqrt{f^{2}-c}$ |
| Parametric Equations of a Circle | $x=h+r \cos \theta ; y=k+r \sin \theta$ |
| Tangent | - Slope form: $y=m x \pm a \sqrt{1+m^{2}}$ <br> - Point form: $x x_{1}+y y_{1}=a^{2}$ or $T=0$ <br> - Parametric form: $x \cos \alpha+y \sin \alpha=a$ |
| Pair of Tangents from a Point: | $S S_{1}=T^{2}$ |


| Length of a Tangent | $\sqrt{S_{1}}$ |
| :---: | :---: |
| Director Circle | $x^{2}+y^{2}=2 a^{2}$ for $x^{2}+y^{2}=a^{2}$ |
| Chord of Contact | $T=0$ <br> i. Length of chord of contact $=\frac{2 L R}{\sqrt{R^{2}+L^{2}}}$ <br> ii. Area of the triangle formed by the pair of the tangents and its chord of contact $=\frac{R L^{3}}{R^{2}+L^{2}}$ <br> iii. Tangent of the angle between the pair of tangents from $\left(x_{1}, y_{1}\right)=\left(\frac{2 R L}{L^{2}-R^{2}}\right)$ <br> iv. Equation of the circle circumscribing the triangle $P T_{1}, T_{2}$ is: $\left(x-x_{1}^{2}\right)(x+g)+\left(y-y_{1}\right)(y+f)=0$ |
| Condition of orthogonality of Two Circles | $2 g_{1} g_{2}+2 f_{1} f_{2}=c_{1}+c_{2}$ |
| Radical Axis | $S_{1}-S_{2}=0$ i.e. $2\left(g_{1}-g_{2}\right) x+2\left(f_{1}-f_{2}\right) y+\left(c_{1}-c_{2}\right)=0$. |
| Family of Circles | $S_{1}+K S_{2}=0, S+K L=0$ |
| Quadratic Equation Formula <br> The formula for quadratic equation are as stated below |  |
| Description | Formula |
| General form of Quadratic Equation | $a x^{2}+b x+c=0 ;$ where $a, b, c$ are constants and $a \neq 0$. |
| Roots of equations | $\alpha=\frac{-b+\sqrt{b^{2}-4 a c}}{2 a}, \beta=\frac{-b-\sqrt{b^{2}-4 a c}}{2 a}$ |
| Sum and Product of Roots | If $\alpha$ and $\beta$ are the roots of the quadratic equation $a x^{2}+b x+c=0$, then <br> Sum of roots, $\alpha+\beta=-\frac{b}{a}$ <br> Product of roots, $\alpha \beta=\frac{c}{a}$ |
| Discriminant of Quadratic equation | The Discriminant of the quadratic equation $a x^{2}+b x+c=0$ is given by $D=b^{2}-4 a c$. |
| Nature of Roots | - If $D=0$, the roots are real and equal $\alpha=\beta=-\frac{b}{2 a}$. |


|  | - If $D \neq 0$, The roots are real and unequal. <br> - If $D<0$, the roots are imaginary and unequal. <br> - If $D>0$ and $D$ is a perfect square, the roots are rational and unequal. <br> - If $D>0$ and $D$ is not a perfect square, the roots are irrational and unequal. |
| :---: | :---: |
| Formation of Quadratic Equation with given roots | If $\alpha$ and $\beta$ are the roots of the quadratic equation, then $(x-\alpha)(x-\beta)=0 ; x^{2}-(\alpha+\beta) x+\alpha \beta=0 ;$ <br> - $x^{2}-($ Sum of roots $) x+$ product of roots $=0$ |
| Common Roots | - If two quadratic equations $a_{1} x^{2}+b_{1} x+c_{1}=0 \&$ $a_{2} x^{2}+b_{2} x+c_{2}=0$ have both roots common, then $\frac{a_{1}}{a_{2}}=\frac{b_{1}}{b_{2}}=\frac{c_{1}}{c_{2}}$. <br> - If only one root $\alpha$ is common, then $\alpha=\frac{c_{1} a_{2}-c_{2} a_{1}}{a_{1} b_{2}-a_{2} b_{1}}=\frac{b_{1} c_{2}-b_{2} c_{1}}{c_{1} a_{2}-c_{2} a_{1}}$ |
| Range of Quadratic Expression $f(x)=a x^{2}+b x+c \text { in }$ <br> restricted domain $x \in\left[x_{1}, x_{2}\right]$ | - If $-\frac{b}{2 a}$ not belong to $\left[x_{1}, x_{2}\right]$ then, <br> $f(x) \in\left[\left\{f\left(x_{1}\right), f\left(x_{2}\right)\right\}, \quad \max \left\{f\left(x_{1}\right), f\left(x_{2}\right)\right\}\right]$ <br> - If $-\frac{b}{2 a} \in\left[x_{1}, x_{2}\right]$ then, $f(x) \in\left[\left\{f\left(x_{1}\right), f\left(x_{2}\right),-\frac{D}{4 a}\right\}, \quad \max \left\{f\left(x_{1}\right), f\left(x_{2}\right),-\frac{D}{4 a}\right\}\right]$ |
| Roots under special cases | Consider the quadratic equation $a x^{2}+b x+c=0$ <br> - If $c=0$, then one root is zero. Other root is $-\frac{b}{a}$. <br> - If $b=0$ The roots are equal but in opposite signs. <br> - If $b=c=0$, then both roots are zero. <br> - If $a=c$, then the roots are reciprocal to each other. <br> - If $a+b+c=0$, then one root is 1 and the second root is $\frac{c}{a}$. <br> - If $a=b=c=0$, then the equation will become an identity and will satisfy every value of $x$. |
| Graph of Quadratic equation | The graph of a quadratic equation $a x^{2}+b x+c=0$ is a parabola. <br> - If $a>0$, then the graph of a quadratic equation will be concave upwards. <br> - If $a<0$, then the graph of a quadratic equation will be concave downwards. |


| Maximum and Minimum value | Consider the quadratic expression $a x^{2}+b x+c=0$ <br> - If $a<0$, then the expression has the greatest value at $x=-\frac{b}{2 a}$. The maximum value is $-\frac{D}{4 a}$. <br> - If $a>0$, then the expression has the least value at $x=-\frac{b}{2 a}$. The minimum value is $-\frac{D}{4 a}$. |
| :---: | :---: |
| Quadratic Expression in Two Variables | The general form of a quadratic equation in two variables $x$ and $y$ is $a x^{2}+2 h x y+b y^{2}+2 g x+2 f y+c$. <br> To solve the expression into two linear rational factors, the condition is $\Delta=0$ <br> [ahg] $\Delta=\left[\begin{array}{lll} \mathrm{h} & \mathrm{~b} \end{array}\right]=0$ <br> [ $\mathrm{g} f \mathrm{c}$ ] <br> $a b c+2 f g h-a f^{2}-b g^{2}-c h^{2}=0$ And $h^{2}-a b>0$. This is called the Discriminant of the given expression. |
| Quick formula revision for jee m | Binomial Theorem Formula <br> ins and advanced. |
| Description | Formula |
| Binomial Theorem for positive Integral Index | $\begin{aligned} & (x+a)^{n}={ }^{\mathrm{n}} \mathrm{C}_{0^{n} a^{0}{ }^{0}+{ }^{\mathrm{n}} \mathrm{C}_{1 x^{n-1} a}+{ }^{\mathrm{n}} \mathrm{C}_{2 x^{n-2}} a^{2}+\ldots+{ }^{\mathrm{n}} \mathrm{C}_{\mathrm{rx}}{ }^{n-r} a^{r}+\ldots+{ }^{\mathrm{n}} \mathrm{C}_{n} \cdot x a^{n}} \\ & \text { General terms }=T_{r+1}={ }^{\mathrm{n}} \mathrm{C}_{r x^{n-r}} a^{r} \end{aligned}$ |
| Deductions of Binomial Theorem | - $(1+x)^{n}={ }^{n} C_{0+}{ }^{n} C_{1 x}+{ }^{n} C_{2 x^{2}}+{ }^{n} C_{3 x^{3}}+\ldots+{ }^{n} C_{r x}{ }^{r}+\ldots+{ }^{n} C_{n x^{n}}$ which is the standard form of binomial expansion. <br> General Term $=(r+1)^{t h}$ term: $T_{r+1}={ }^{n} C_{r}$ <br> $x^{r}=\frac{n(n-1)(n-2) \ldots . .(n-r+1)}{n} \cdot x^{r}$ <br> - $(1-x)^{n}=^{n} C_{0-}{ }^{n} C_{1 x}+{ }^{n} C_{2 x^{2}}{ }^{n}{ }^{n} C_{3 x} x^{3}+\ldots+(-1)^{n} \mathrm{C}_{r x}+\ldots+(-1)^{n}{ }^{n} C_{n x}{ }^{n}$ General Term $=(r+1)^{t h}$ term: $T_{r+1}=(-1)^{r} .{ }^{n} C_{r}$ $x^{r}=\frac{n(n-1)(n-2) \ldots(n-r+1)}{n} \cdot x^{r}$ |
| Middle Term in the expansion of $(x+a)^{n}$ | - If $n$ is even then middle term $=\left(\frac{n}{2}+1\right)^{\text {th }}$ term. <br> - If $n$ is odd then middle terms are $\left(\frac{n+1}{2}\right)^{t h}$ and $\left(\frac{n+3}{2}\right)^{t h}$ term. <br> - Binomial coefficients of middle term is the greatest Binomial coefficients |


| To determine a particular term in the expansion | In the expansion of $\left(x^{\alpha} \pm \frac{1}{x^{\beta}}\right)^{n}$, if $x^{m}$ occurs in $T_{r+1}$, then $r$ is given by $n \alpha-r(\alpha+\beta)=m \Rightarrow r=\frac{n \alpha-m}{\alpha+\beta}$ and the term which is independent of $x$ then $n \alpha-r(\alpha+\beta)=0 \Rightarrow r=\frac{n \alpha}{\alpha+\beta} .$ |
| :---: | :---: |
| To find a term from the end in the expansion of $(x+a)^{n}$ | $T_{r}(E)=T_{n-r+2}(B)$ |
| Binomial Coefficients and their properties | In the expansion of $(1+x)^{n}=C_{0}+C_{1} x+C_{2} x^{2}+\ldots+C_{r} x^{r}+\ldots+C_{n} x^{n}$ <br> Where $C_{0}=1, C_{1}=n, C_{2}=\frac{n(n-1)}{2!}$ <br> i. $C_{0}+C_{1}+C_{2}+\ldots \ldots+C_{n}=2^{n}$ <br> ii. $C_{0}-C_{1}+C_{2}-C_{3}+\ldots \ldots=0$ <br> iii. $C_{0}+C_{2}+\ldots \ldots=C_{1}+C_{3}+\ldots \ldots=2^{n-1}$ <br> iv. $\quad C_{0}^{2}+C_{1}^{2}+C_{2}^{2}+\ldots \ldots+C_{n}^{2}=\frac{2 n!}{n!n!}$ <br> v. $\quad C_{0}+\frac{C_{1}}{2}+\frac{C_{2}}{3}+\ldots \ldots+\frac{C_{n}}{n+1}=\frac{2^{n+1}-1}{n+1}$ <br> vi. $\quad C_{0}-\frac{C_{1}}{2}+\frac{C_{2}}{3}-\frac{C_{3}}{4}+\ldots \ldots+\frac{(-1)^{n} \cdot C_{n}}{n+1}=\frac{1}{n+1}$ |
| Greatest term in the expansion of $(x+a)^{n}$ : | - The term in the expansion of $(x+a)^{n}$ of greatest coefficients $\begin{aligned} & =\left\{T_{\frac{(n+2)}{2},} \quad \text { when } n \text { is even } T_{\frac{(n+1)}{2},}, T_{\frac{(n+3)}{2}}\right. \\ & \text { when is is odd } \end{aligned}$ <br> - The greatest term $=\left\{T_{p}, T_{p+1}, \text { when } \frac{(n+1) a}{x+a}=p \in Z T_{q+1,}\right.$ <br> When $\frac{(n+1) a}{x+1}$ nnot belong to $Z$ and $q<\frac{(n+1) a}{x+a}<q+1$ |
| Multinomial Expansion | If $n \in N$ then the general terms of multinomial expansion $\left(x_{1}+x_{2}+x_{3}+\ldots+x_{k}\right)^{n}$ is $\sum_{r_{1}+r_{2}+\ldots+r_{k}=n} \frac{n!}{r_{1}!r_{2}!\ldots r_{k} r_{1}} x_{1}^{r 1} \cdot x_{2}^{r 2} \ldots x_{k}^{r_{k}}$ |


| Binomial Theorem for | $(1+x)^{n}=1+n x+\frac{n(n-1)}{2!} x^{2}+\frac{n(n-1)(n-2)}{3!} x^{3}+\ldots$ |
| :--- | :--- |
| Negative Integer Or | $+\frac{n(n-1)(n-2) \ldots \ldots .(n-r+1)}{r!} x^{r}+\ldots,\|x\|<1$ |
| Fractional Indices | $T_{r+1}=\frac{n(n-1)(n-2) \ldots \ldots .(n-r+1)}{r!} x^{r}$ |
|  |  |

## Part 2

## Vectors Formula

The formula for vectors are as stated below

| Description | Formula |
| :---: | :---: |
| Position Vector of a Point | If $\vec{a}$ and $\vec{b}$ are positive vectors of two points $A$ and $B$, then $\overrightarrow{A B}=\vec{b}-\vec{a}$ <br> - Distance Formula: Distance between the two points $A(\vec{a})$ and $B(\vec{b})$ is $A B=\|\vec{a}-\vec{b}\|$ <br> - Section Formula: $\vec{r}=\frac{n \vec{a}+m \vec{b}}{m+n}$, Midpoint of $A B=\frac{\vec{a}+\vec{b}}{2}$ |
| Scalar Product of Two vectors | $\vec{a} \cdot \vec{b}=\|\vec{a}\|\|\vec{b}\| \cos \theta$, where $\|\vec{a}\|,\|\vec{b}\|$ are the magnitude of $\vec{a}$ and $\vec{b}$ respectively and $\theta$ is the angle between $\vec{a}$ and $\vec{b}$ <br> - $i . i=j . j=k . k=1 ; i . j=j . k=k . i=0$, projection of $\vec{a}$ on $\vec{b}=\frac{\vec{a} \cdot \vec{b}}{\|\vec{b}\|}$. <br> - If $\vec{a}=a_{1} i+a_{2} j+a_{3} k \quad \& \quad \vec{b}=b_{1} i+b_{2} j+b_{3} k$ then $\vec{a} \cdot \vec{b}=a_{1} b_{1}+a_{2} b_{2}+a_{3} b_{3}$. <br> - The angle $\emptyset$ between $\vec{a}$ \& $\vec{b}$ is given by $\emptyset=\cos ^{-1} \frac{\vec{a} \cdot \vec{b}}{\|\vec{a}\|\|\vec{b}\|}, 0 \leq \varnothing \leq \pi$. <br> - $\vec{a} \cdot \vec{b}=0 \Leftrightarrow \vec{a}$ Perpendicular to $\vec{b} \quad(\vec{a} \neq 0, \vec{b} \neq 0)$. |


| Vector Product of Two vectors | - If $\vec{a} \& \vec{b}$ are two vectors and $\theta$ is the angle between them then <br> - $\vec{a} \times \vec{b}=\|\vec{a}\|\|\vec{b}\| \sin \theta \hat{n}, \underset{\rightarrow}{\text { where }} \hat{n}$ is the unit vector perpendicular to both $\vec{a} \& \vec{b}$ such that $\vec{a}, \vec{b} \& \hat{n}$ form a right handed screw system. <br> - Geometrically $\|\vec{a} \times \vec{b}\|=$ area of the parallelogram whose two adjacents sides are represented by $\vec{a} \& \vec{b}$. <br> - $\hat{i} \times \hat{i}=\hat{j} \times \hat{j}=\hat{k} \times \hat{k}=0 ; \hat{i} \times \hat{j}=\hat{k}, \hat{j} \times \hat{k}=\hat{i}, \hat{k} \times \hat{i}=\hat{j}$ <br> - If $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ <br> $\& \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k} \quad$ then $\vec{a} \times \vec{b}=\left\|\begin{array}{ccc} \hat{i} & \hat{j} & \hat{k} \\ a_{1} & a_{2} & a_{3} \\ b_{1} & b_{2} & b_{3} \end{array}\right\|$ <br> - $\vec{a} \times \vec{b}=\vec{o} \leftrightarrow \vec{a}$ and $\vec{b}$ are parallel (collinear) $(\vec{a} \neq 0, \vec{b} \neq 0)$ i.e. $\vec{a}=K \vec{b}$ where $K$ is a scalar. <br> - Unit vector perpendicular to the plane of $\vec{a} \& \vec{b}$ is $\begin{aligned} & \hat{n}= \pm \frac{\vec{a} \times \vec{b}}{\|\vec{a} \times \vec{b}\|} . \\ & \rightarrow \vec{\rightarrow},\end{aligned}$ <br> - If $\vec{a}, \vec{b} \& \vec{c}$ are the position vectors of 3 points $\mathrm{A}, \mathrm{B} \& \mathrm{C}$ then the vector area of triangle $A B C=\frac{1}{2}[\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}]$. The points $\mathrm{A}, \mathrm{B} \& \mathrm{C}$ are collinear if <br> - $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=\overrightarrow{0}$ <br> - Area of any quadrilateral whose diagonal vectors are $\vec{d}_{1} \& \vec{d}_{2}$ is given by $\frac{1}{2}\left\|\overrightarrow{d_{1}} \times \vec{d}_{2}\right\|$. <br> - Lagrange'sIdentity: $(\vec{a} \times \vec{b})^{2}=\|\vec{a}\|^{2}\|\vec{b}\|^{2}-(\vec{a} \cdot \vec{b})^{2}=[(\vec{a} \times \vec{a})(\vec{a} \times \vec{b})(\vec{b} \times \vec{a})(\vec{b}$ |
| :---: | :---: |
| Scalar Triple Product | - The scalar triple product of three vectors $\vec{a}, \vec{b} \& \vec{c}$ is defined as: $\vec{a} \times \vec{b} \cdot \vec{c}=\|\vec{a}\|\|\vec{b}\|\|\vec{c}\| \sin \sin \theta \cos \cos \emptyset$ <br> - Volume of tetrahedron $V=[\vec{a} \cdot \vec{b} \cdot \vec{c}]$ <br> - In a scalar triple product the position of dot and cross can be interchanged i.e. |


|  | $\vec{a} \cdot(\vec{b} \times \vec{c})=(\underset{\rightarrow}{\vec{a} \times \vec{b}}) \cdot \vec{c}$ Or $\left[\begin{array}{ll}\vec{a} & \vec{b} \\ \vec{a}\end{array}\right]=\left[\begin{array}{lll}\vec{b} & \vec{c} & \vec{a}\end{array}\right]=\left[\begin{array}{lll}\vec{c} & \vec{a} & \vec{b}\end{array}\right]$ <br> $\vec{a} .(\vec{b} \times \vec{c})=-\vec{a} \cdot(\vec{c} \times \vec{b})$ i.e. $[\vec{a} \vec{b} \vec{c}]=-[\vec{a} \vec{c} \vec{b}]$ <br> - If $\vec{a}=a_{1} i+a_{2} j+a_{3} k ; \vec{b}=b_{1} i+b_{2} j+b_{3} k$ $\vec{c}=c_{1} i+c_{2} j+c_{3} k$ then $[\vec{a} \cdot \vec{b} \cdot \vec{c}]=\left[\begin{array}{ccc} a_{1} & a_{2} & a_{3} \\ b_{1} & b_{2} & b_{3} \\ c_{1} & c_{2} & c_{3} \end{array}\right]$ <br> - If $\vec{a}, \vec{b}, \vec{c}$ are coplanar $\leftrightarrow[\vec{a} \vec{b} \vec{c}]=0$. <br> - Volume of tetrahedron OABC with O as origin \& $\mathrm{A}(\vec{a}), \mathrm{B}(\vec{b})$ and $C(\vec{c})$ be the vertices $=\left\|\frac{1}{6}[\vec{a} \vec{b} \vec{c}]\right\|$. <br> - The position vector of the centroid of a tetrahedron if the pv's of its vertices are $\vec{a}, \vec{b}, \vec{c} \& \vec{d}$ are given by $\frac{1}{4}[\vec{a}+\vec{b}+\vec{c}+\vec{d}]$. |
| :---: | :---: |
| Vector Triple Product | $\begin{aligned} & \vec{a} \times(\vec{b} \times \vec{c})=(\vec{a} \cdot \vec{c}) \vec{b}-(\vec{a} \cdot \vec{b}) \vec{c},(\vec{a} \times \vec{b}) \times \vec{c}=(\vec{a} \cdot \vec{c}) \vec{b}-(\vec{b} \cdot \vec{c}) \vec{a} \\ & \text { In general: }(\vec{a} \times \vec{b}) \times \vec{c} \neq \vec{a} \times(\vec{b} \times \vec{c}) \end{aligned}$ |
|  | Parabola Formula <br> The formula for parabola are as stated below |
| Description | Formula |
| Equation of standard parabola: $\qquad$ | The equation of parabola with focus at ( $a, 0$ ), $a>0$ and directrix $x=-a$ is given as $y^{2}=4 a x$ <br> When vertex is $(0,0)$ then axis is given as $y=0$ <br> Length of latus rectum is equals to $4 a$ <br> Ends of the latus rectum are $\mathrm{L}(\mathrm{a}, 2 \mathrm{a})$ and $\mathrm{L}^{\prime}(\mathrm{a},-2 \mathrm{a})$. |
| Parametric representation | The point $\left(x, y_{1}\right)$ lies outside, on or inside the parabola which is given as $y=4 a x$ <br> Therefore, equation of parabola now becomes, $y_{1}^{2}-4 a x \geq 0$ <br> Or $y_{1}^{2}-4 a x<0$ |
| Line and a parabola | Length of the chord intercepted by the parabola $y^{2}=4 a x$ on the line $y=m x+c$ is given as |


|  | $\frac{4}{m^{2}}\left(\sqrt{a\left(1+m^{2}\right)(a-m c)}\right.$ |
| :---: | :---: |
| Tangents to the parabola | $\begin{aligned} & \hline \text { Tangent of the parabola } y^{2}=4 a x \text { is given as } \mathrm{T}=0 \\ & y=m x+\frac{a}{m}, m \neq 0 \text { is the tangent of parabola } y^{2}=4 a x \text { at }\left(\frac{a}{m^{2}}, \frac{2 a}{m}\right) \\ & \hline \end{aligned}$ |
| Normal to the parabola $y^{2}=4 a x$ | Normal to the parabola $y^{2}=4 a x$ is given as $y-y_{1}=\frac{-y_{1}}{2 a}\left(x-x_{1}\right) \text { at }\left(x_{1}, y_{1}\right)$ |
| A chord with a given middle point | The equation of the chord of parabola $y^{2}=4 a x$ with midpoint $\left(x_{1}, y_{1}\right)$ is given as $T=S_{1}$. <br> Here, $S_{1}=y_{1}-4 a x$ |
| The formula for de | Definite Integration Formula <br> finite integration are as stated below |
| Description | Formula |
| Definite Integral as Limit Sum | $\int_{a}^{b} f(x) d x=\sum_{r=1}^{n} h f(a+r h)$ <br> Here $h=\frac{b-a}{n}$ is the length of each subinterval |
| Definite Integral Formula Using the Fundamental theorem of calculus | $\int_{a}^{b} f(x) d x=F(b)-F(a)$, where $F^{\prime}(x)=f(x)$ |
| Properties of Definite Integral | - $\int_{a}^{b} f(x) \cdot d x=\int_{a}^{b} f(t) \cdot d t$ <br> - $\int_{a}^{b} f(x) \cdot d x=-\int_{b}^{a} f(x) \cdot d x$ <br> - $\int_{a}^{b} c f(x) \cdot d x=c \int_{a}^{b} f(x) \cdot d x$ <br> - $\int_{a}^{b} f(x) \pm g(x) \cdot d x=\int_{a}^{b} f(x) \cdot d x \pm \int_{a}^{b} g(x) \cdot d x$ <br> - $\int_{a}^{b} f(x) \cdot d x=\int_{a}^{c} f(x) \cdot d x+\int_{c}^{b} f(x) \cdot d x$ <br> - $\int_{a}^{b} f(x) \cdot d x=\int_{a}^{b} f(a+b-x) \cdot d x$ |


|  | - $\int_{0}^{a} f(x) \cdot d x=\int_{0}^{a} f(a-x) \cdot d t \quad$ This is a formula derived from the above formula. <br> - $\int_{0}^{2 a} f(x) \cdot d x=2 \int_{0}^{a} f(x) \cdot d x$ if $f(2 a-x)=f(x)$ <br> - $\int_{0}^{2 a} f(x) \cdot d x=0$ if $f(2 a-x)=-f(x)$ <br> - $\int_{-a}^{a} f(x) \cdot d x=2 \int_{0}^{a} f(x) \cdot d x$ if $f(x)$ is an even function (i.e., $f(-x)=f(x))$. <br> - $\int_{-a}^{a} f(x) \cdot d x=0$ if $f(x)$ is an odd function (i.e., $f(-x)=-f(x))$. |
| :---: | :---: |
| Definite <br> Integrals <br> involving <br> Rational <br> irrational <br> Expression | - $\int_{a}^{\infty} \frac{d x}{x^{2}+a^{2}}=\frac{\pi}{2 a}$ <br> - $\int_{a}^{\infty} \frac{x^{m} d x}{x^{n}+a^{n}}=\frac{\pi a^{m-n+1}}{\left.n \frac{(m+1) \pi}{n}\right)}, 0<m+1<n$ <br> - $\int_{a}^{\infty} \frac{x^{p-1} d x}{1+x}=\frac{\pi}{\sin \sin (p \pi)}, 0<p<1$ <br> - $\int_{a}^{\infty} \frac{d x}{\sqrt{a^{2}-x^{2}}}=\frac{\pi}{2}$ <br> - $\int_{a}^{\infty} \sqrt{a^{2}-x^{2}} d x=\frac{\pi a^{2}}{4}$ |
| Definite <br> Integrals involving <br> Trigonometric Functions | - $\left.\left.\int_{0}^{\pi} m x\right) n x\right) d x=\left\{0\right.$ if $m \neq n \frac{\pi}{2}$ if $m=n \quad m, n \quad$ positive integers <br> - $\left.\left.\int_{0}^{\pi} m x\right) n x\right) d x=\left\{0\right.$ if $m \neq n \frac{\pi}{2}$ if $m=n \quad m, n \quad$ positive integers <br> - $\left.\left.\int_{0}^{\pi} m x\right) n x\right) d x=\left\{0 \quad\right.$ if $m+n$ even $\frac{2 m}{m^{2}-n^{2}}$ if $m=n$ integers |


|  | - $\int_{0}^{\frac{\pi}{2}} x d x=\int_{0}^{\frac{\pi}{2}} x d x=\frac{\pi}{4}$ <br> - $\int_{0}^{\frac{\pi}{2}} x d x=\int_{0}^{\frac{\pi}{2}} d x=\frac{1.3 .5 \ldots \ldots \ldots .2 m-1}{2.4 .6 \ldots . .2 m} \cdot \frac{\pi}{2}, m=1,2, \ldots$ <br> - $\int_{0}^{\frac{\pi}{2}} x d x=\int_{0}^{\frac{\pi}{2}} d x=\frac{2.4 .6 \ldots \ldots 2 m}{1.3 .5 \ldots .2 m+1}, m=1,2, \ldots$ |
| :---: | :---: |
| If $f(x)$ is a periodic function with period T | - $\int_{0}^{n} f(x) d x=n \int_{0}^{T} f(x) d x, n \in z, \int_{a}^{a+n T} f(x) d x=n \int_{0}^{T} f(x) d x, n \in z$ <br> - $\int_{m T}^{n T} f(x) d x=(n-m) \int_{0}^{T} f(x) d x, m, n \in z, \int_{n T}^{a+n T} f(x) d x=\int_{0}^{a} f($ <br> - $\int_{a+n T}^{b+n T} f(x) d x=\int_{a}^{a} f(x) d x, n \in z, \quad a, b \in R$ |
| Leibnitz <br> Theorem | If $F(x)=\int_{g(x)}^{h(x)} f(t) d t$, then $\frac{d F(x)}{d x}=h^{\prime}(x) f(h(x))-g^{\prime}(x) f(g(x))$ |

## Ellipse Formula

The formula for ellipse are as stated below

| Description | Formula |
| :---: | :---: |
| Standard Equation | $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$, where $a>\& b^{2}=a^{2}\left(1-e^{2}\right)$ <br> - Eccentricity: $e=\sqrt{1-\frac{b^{2}}{a^{2}}},(0<e<1)$, Directrices: $x= \pm \frac{a}{e}$ <br> - Foci: $S=( \pm a e, 0)$. Length of major axes $=2 a$ and minor axes $=2 b$ <br> - Vertices: $A=(-a, 0) \& A=(a, 0)$. <br> - Latus Rectum: $=\frac{2 b^{2}}{a}=2 a\left(1-e^{2}\right)$ |


| Auxiliary circle | $x^{2}+y^{2}=a^{2}$ |
| :---: | :---: |
| Parametric Representation | $x=a \cos \theta \& y=b \sin \theta$ |
| Position of a Point w.r.t. an Ellipse | The point $\mathrm{P}\left(x_{1}, y_{1}\right)$ lies outside, inside or on the ellipse according as; $\frac{x_{1}^{2}}{a^{2}}+\frac{y_{1}^{2}}{b^{2}}-1><\text { or }=0 .$ |
| Line and an Ellipse | The line $y=m x+c$ meets the ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$ in two points real, coincident or imaginary according as $c^{2}$ is $<=o r>a^{2} m^{2}+b^{2}$. |
| Tangents | - Slope form: $y=m x \pm \sqrt{a^{2} m^{2}+b^{2}}$, point form: $\frac{x x_{1}}{a^{2}}+\frac{y y_{1}}{b^{2}}=1$ <br> - Parametric form: $\frac{x \cos \theta}{a}+\frac{y \sin \theta}{b}=1$ |
| Normal | $\begin{aligned} & \frac{a^{2} x}{x_{1}}-\frac{b^{2} y}{y_{1}}=a^{2}-b^{2}, a x \cdot \sec \theta-b y \cdot \operatorname{cosec} \theta=\left(a^{2}-b^{2}\right), \\ & y=m x-\frac{\left(a^{2}-b^{2}\right) m}{\sqrt{a^{2}+b^{2}} m^{2}} \end{aligned}$ |
| Director Circle | $x^{2}+y^{2}=a^{2}+b^{2}$ |

## Part 3

## Inverse Trigonometric Functions Formula

The formula for inverse trigonometric functions are as stated below

| Description | Formula |
| :--- | :--- |
| Arcsine Function | Arcsine function is an inverse of sine function which is denoted by <br> $\sin ^{-1}$ <br> The formula for arcsin is given as <br> $\sin ^{-1}(-x)=-\sin ^{-1}(x), x \in[-1,1]$ |


|  | Domain of arcsin is $-1 \leq x \leq 1$ <br> Range of $\arcsin$ is $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$ <br> Differentiation of $\sin ^{-1}(x)$ is $\frac{1}{\sqrt{1-x^{2}}}$ |
| :---: | :---: |
| Arccosine Function | Arccosine function is an inverse of cosine function which is denoted by $\cos ^{-1}$ $\cos ^{-1}(-x)=\pi-\cos ^{-1}(x), x \in[-1,1]$ <br> Domain of arccos is $-1 \leq x \leq 1$ <br> Range of arccos is $0 \leq y \leq \pi$ <br> Differentiation of $\cos ^{-1}(x)$ is $-\frac{1}{\sqrt{1-x^{2}}}$ |
| Arctangent Function | Arctangent function is an inverse of tangent function which is denoted by $\tan ^{-1}$ $\tan ^{-1}(-x)=-\tan ^{-1}(x), x \in R$ <br> Domain of Arctangent is $-\infty \leq x \leq \infty$ <br> Range of Arctangent is $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$ |


|  |  <br> Differentiation of $\tan ^{-1}(x)$ is $\frac{1}{1+x^{2}}$ |
| :---: | :---: |
| Arc cotangent (Arc cot) Function | Arc cotangent function is an inverse of cotangent function which is denoted by $\cot ^{-1}$ $\cot ^{-1}(-x)=\pi-\cot ^{-1}(x), x \in R$ <br> Domain of Arc cotangent is $-\infty \leq x \leq \infty$ <br> Range of Arc cotangent is $0 \leq y \leq \pi$ <br> Differentiation of $\cot ^{-1}(x)$ is $\frac{-1}{1+x^{2}}$ |
| Arc secant Function | Arc secant function is an inverse of cosine function which is denoted by $\cot ^{-1}$ $\sec ^{-1}(-x)=\pi-\sec ^{-1}(x),\|x\| \geq 1$ <br> Domain of Arc secant is $-\infty \leq x \leq-1$ or $1-\infty \leq x \leq-\infty$ Range of Arc secant is $0 \leq y \leq \pi, y \neq \frac{\pi}{2}$ |


|  |  <br> Differentiation of $\sec ^{-1}(x)$ is $\frac{-1}{\|x\| \sqrt{x^{2}-1}}$ |
| :---: | :---: |
| Arc cosecant Function | Arc cosecant function is an inverse of sine function which is denoted by $\operatorname{cosec}^{-1}$ $\operatorname{cosec}^{-1}(-x)=-\operatorname{cosec}^{-1}(x), x \geq 1$ <br> Domain of Arc cosecant is $-\infty \leq x \leq-1$ or $1-\infty \leq x \leq-\infty$ <br> Range of Arc cosecant is $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}, y \neq 0$ <br> Differentiation of $\operatorname{cosec}^{-1}(x)$ is $\frac{1}{\|x\| \sqrt{x^{2}-1}}$ |
| Straight Line Formula <br> The formula for straight line are as stated below |  |
| Description | Formulas |
| Distance Formula | $d=\sqrt{\left(x_{1}-x_{2}\right)^{2}-\left(y_{1}-y_{2}\right)^{2}}$ |
| Section Formula | $x=\frac{m x_{2} \pm n x_{1}}{m \pm n} ; y=\frac{m y_{2} \pm n y_{1}}{m \pm n}$ |
| Centroid, Incentre and Excenter | Centroid $G\left(\frac{x_{1}+x_{2}+x_{3}}{3}, \frac{y_{1}+y_{2}+y_{3}}{3}\right)$ |


|  | $\begin{aligned} & \text { In center } I\left(\frac{a x_{1}+b x_{2}+c x_{3}}{a+b+c}, \frac{a y_{1}+b y_{2}+c y_{3}}{a+b+c}\right) \\ & \text { Excentre } I_{1}\left(\frac{-a_{x}+b x_{2}+c x_{3}}{-a+b+c}, \frac{-a y_{1}+b y_{2}+c y_{3}}{-a+b+c}\right) \end{aligned}$ |
| :---: | :---: |
| Area of Triangle | $\triangle A B C=\frac{1}{2}\left\|x_{1} y_{1} 1 x_{2} y_{2} 1 x_{3} y_{3} 1\right\|$ |
| Slope formula | $\begin{array}{r} \text { Line Joining two points }\left(x_{1} y_{1}\right) \&\left(x_{2} y_{2}\right) \\ m=\frac{y_{1}-y_{2}}{x_{1}-x_{2}} \end{array}$ |
| Condition of collinearity of three points | $\left\|x_{1} y_{1} 1 x_{2} y_{2} 1 x_{3} y_{3} 1\right\|=0$ |
| Angle between two straight lines | $\tan \theta=\left\|\frac{m_{1}-m_{2}}{1+m_{1} m_{2}}\right\|$ |
| Bisector of the angles between two lines | $\frac{a x+b y+c}{\sqrt{a^{2}+b^{2}}}= \pm \frac{\left(a^{\prime} x+b^{\prime} y+c^{\prime}\right)}{\sqrt{a^{2}+b^{\prime 2}}}$ |
| Condition of Concurrency | For three lines $a_{1} x+a_{2} y+c_{1}=0, i=123$ is $\left\|a_{1} b_{1} c_{1} a_{2} b_{2} c_{2} a_{3} b_{3} c_{3}\right\|=0$ |
| A pair of straight lines through origin | $a x^{2}+2 h x y+b y^{2}=0$ <br> If $\theta$ is the acute angle between the pair of straight lines, then $\tan \theta$ $=\left\|\frac{2 \sqrt{\left(h^{2}-a b\right)}}{a+b}\right\|$ |
| Two Lines: | $a x+b x+c=0$ and $a x+b y+c=0$ Two lines <br> a. Parallel if $\frac{a}{a^{\prime}}=\frac{b}{b^{\prime}} \neq \frac{c}{c^{\prime}}$ <br> b. Distance between two parallel lines $=\left\|\frac{c_{1}-c_{2}}{\sqrt{a^{2}+b^{2}}}\right\|$ <br> c. Perpendicular: if $a a^{\prime}+b b^{\prime}=0$ |
| A point and line | a. Distance between point and line $=\left\|\frac{a x_{1}+b y_{1}+c}{\sqrt{a^{2}+b^{2}}}\right\|$ <br> b. Reflection of a point about a line: $\frac{x-x_{1}}{a}=\frac{y-y_{1}}{b}=-2 \frac{a x_{1}+b y_{1}+c}{a^{2}+b^{2}}$ <br> c. Foot of the perpendicular from a point on the line is $\frac{x-x_{1}}{a}=\frac{y-y_{1}}{b}=-\frac{a x_{1}+b y_{1}+c}{a^{2}+b^{2}}$ |

## Indefinite Integration formula

The formula for indefinite integration are as stated below

## If $\mathbf{f} \boldsymbol{\&} \mathbf{g}$ are functions of $\mathbf{x}$ such that

$g(x)=f(x)$ then,
$\int f(x) d x=g(x)+c \Leftrightarrow \frac{d}{d x}\{g(x)+c\}=f(x)$
Here, c is called the constant of integration

Standard Formula:

- $\int(a x+b)^{n} d x=\frac{(a x+b)^{n+1}}{a(n+1)}+c, n \neq-1$
- $\int \frac{d x}{a x+b}=\frac{1}{a} \ln \ln (a x+b)+c$
- $\int e^{a x+b} d x=\frac{1}{a} e^{a x+b}+c$
- $\int a^{p x+q} d x=\frac{1}{P} \frac{a^{p x+q}}{\ln l n a}+c$, Here $a>0$
- $\int \sin (a x+b) d x=-\frac{1}{a} \cos \cos (a x+b)+c$
- $\int \cos (a x+b) d x=\frac{1}{a} \sin \sin (a x+b)+c$
- $\int \tan (a x+b) d x=\frac{1}{a} \ln \ln \sec \sec (a x+b)+c$
- $\int \cot (a x+b) d x=\frac{1}{a} \ln \ln \sin \sin (a x+b)+c$
- $\int(a x+b) d x=\frac{1}{a} \tan (a x+b)+c$
- $\int(a x+b) d x=-\frac{1}{a} \cot (a x+b)+c$
- $\int d x=\ln (\sec x+\tan x)+c$
or $\int d x=\ln \tan \left(\frac{\pi}{4}+\frac{x}{2}\right)+c$

|  | - $\int d x=\ln (x+\cot x)+c$ or $\int d x=\ln \tan \frac{x}{2}+c$ <br> or $\int d x=\ln (\operatorname{cosec} x+\cot x)+c$ <br> - $\int \frac{d x}{\sqrt{a^{2}-x^{2}}}=\frac{x}{a}+c$ <br> - $\int \frac{d x}{a^{2}+x^{2}}=-\frac{1}{a} \frac{x}{a}+c$ <br> - $\int \frac{d x}{\|x\| \sqrt{x^{2}+a^{2}}}=-\frac{1}{a} \frac{x}{a}+c$ <br> - $\int \frac{d x}{\sqrt{x^{2}+a^{2}}}=\ln \left[x+\sqrt{x^{2}+a^{2}}\right]+c$ <br> - $\int \frac{d x}{\sqrt{x^{2}-a^{2}}}=\ln \left[x+\sqrt{x^{2}-a^{2}}\right]+c$ <br> - $\int \frac{d x}{a^{2}-x^{2}}=\frac{1}{2 a} \ln \left\|\frac{a+x}{a-x}\right\|+c$ <br> - $\int \frac{d x}{x^{2}-a^{2}}=\frac{1}{2 a} \ln \left\|\frac{x-a}{x+a}\right\|+c$ <br> - $\int \sqrt{a^{2}-x^{2}} d x=\frac{x}{2} \sqrt{x^{2}+a^{2}}+\frac{a^{2}}{2} \frac{x}{a}+c$ <br> - $\int \sqrt{x^{2}+a^{2}} d x=\frac{x}{2} \sqrt{x^{2}+a^{2}}+\frac{a^{2}}{2} \ln \left(\frac{x+\sqrt{x^{2}+a^{2}}}{a}\right)+c$ <br> - $\int \sqrt{x^{2}-a^{2}} d x=\frac{x}{2} \sqrt{x^{2}-a^{2}}-\frac{a^{2}}{2} \ln \left(\frac{x+\sqrt{x^{2}-a^{2}}}{a}\right)+c$ |
| :---: | :---: |
| Integration by substitutions | If we substitute $f(x)=t$, then $f^{\prime}(x) d x=d t$ |
| Integration by part | $\int(f(x) g(x)) d x=f(x) \int(g(x)) d x-\int\left(\frac{d}{d x}(f(x)) \int(g(x)) d x\right) d x$ |


| Integration of type | $\int \frac{d x}{a x^{2}+b x+c}, \int \frac{d x}{\sqrt{a x^{2}+b x+c}}, \int \sqrt{a x^{2}+b x+c} d x$ <br> Make the substitute $x+\frac{b}{2 a}=t$ |
| :---: | :---: |
| Integration of trigonometric functions | $\int \frac{d x}{a+b x} \text { or } \int \frac{d x}{a+b x} \text { or } \int \frac{d x}{a x+b \sin \sin x \cos \cos x+c x}$ <br> Here we put $\tan \tan x=t$ $\int \frac{d x}{a+b \sin \sin x} \text { or } \int d x /(a+b \cos \cos x) \text { or } \int \frac{d x}{a+b \sin \sin x+c \cos \cos x}$ <br> Here we put $\tan \tan \frac{x}{2}=t$ |
| Integration of type | $\int \frac{x^{2}+1}{x^{4}+K x^{2}+1} d x$ <br> Here $k$ is any constant <br> So, we divide numerator and denominator by $x^{2}$ and put $x \mp \frac{1}{x}=t$ |
| Application of Derivatives Formula <br> The formula for application of derivatives are as stated below |  |
| Description | 1- Formula |
| Equation of tangent and normal | - Tangent at $\left(x_{1}, y_{1}\right)$ is given by $\left(y-y_{1}\right)=f^{\prime}\left(x_{1}\right)\left(x-x_{1}\right)$, here the $f^{\prime}\left(x_{1}\right)$ should be real <br> - And normal at $\left(x_{1}, y_{1}\right)$ is given by $\left(y-y_{1}\right)=-\frac{1}{f^{\prime}\left(x_{1}\right)}\left(x-x_{1}\right)$ , here the $f^{\prime}\left(x_{1}\right)$ should be non-zero and real. |
| Tangent from an external point | Given a point $P(a, b)$ which does not lie on the curve $y=f(x)$, then the equation of possible tangents to the curve $y=f(x)$, passing through $(a, b)$ can be found by solving for the point of contact Q . $f^{\prime}(h)=\frac{f(h)-b}{h-a}$ |




## Part 4

## Sequence \& Series

The formula for sequence and series are as stated below

| Description | Formula |
| :--- | :--- |
| An arithmetic progression (A. P) | a, $a+d, a+2 d, \ldots, a+(n-1) d$ is an <br> A. P. <br> Let a be the first term and $d$ be the common difference of <br> an A. P., <br> then $n^{\text {th }}$ term $=t_{n}=a+(n-1) d$ |


| The sum of first $n$ terms of A. P. | $S_{n}=\frac{n}{2}[2 a+(n-1) d]=\frac{n}{2}[a+l]$ <br> $r^{\text {th }}$ term of an A. P. when sum of first $r$ terms is given is $t_{r}=S_{r}-S_{r}-1$ |
| :---: | :---: |
| Properties of A. P. | - If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in A. P. $\Rightarrow 2 b=a+c \&$ if $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}$ are in A. P. $\Rightarrow a+d=b+c$ <br> - Sum of the terms of an A.P. equidistant from the beginning \& end = sum of first \& last term. |
| Arithmetic Mean | If three terms are in A.P. then the middle term is called the A.M. between the other two, so if $a, b, c$ are in A.P., $b$ is A.M. of a \& c. <br> n - Arithmetic Means between two number <br> If $\mathrm{a}, \mathrm{b}$ are any two given numbers $\& a, A_{1}, A_{2}, \ldots . ., A_{n^{\prime}}, b$ are in A.P. then $A_{1}, A_{2}, \ldots A_{n}$ are the <br> n A.M.'s between $\mathrm{a} \& \mathrm{~b}$. $\begin{aligned} & A_{1}=a+\frac{b-a}{n+1} \\ & A_{2}=a+\frac{2(b-a)}{n+1}, \ldots, A_{n}=a+\frac{n(b-a)}{n+1} \\ & \sum_{r=1}^{n} A_{r}=n A \text { where } A \text { is the single A.M. between } a \& b . \end{aligned}$ |
| Geometric Progression | $a, a r, a r^{2}, a r^{3}, a r^{4}, \ldots$, is a G.P. with a as the first term \& $r$ as a common ratio. <br> - $n^{\text {th }}$ term $=a r^{n-1}$ <br> - Sum of the first $n$ terms i.e., $S_{n}=\left\{\frac{a\left(r^{n}-1\right)}{r-1}, \quad r \neq 1 n a, \quad r=1\right.$ |
| Harmonic Mean | - If $a, b, c$ are in H.P., $b$ is the H.M. between $a \& c$, then $b=\frac{2 a c}{a+c}$ <br> - H.M. of $a_{1}, a_{2} \ldots a_{n}$ is given by $\frac{1}{H}=\frac{1}{n}\left[\frac{1}{a_{1}}+\frac{1}{a_{2}}+\ldots+\frac{1}{a_{n}}\right]$ |
| Relation between means: | $\begin{aligned} & G^{2}=A H, A . M . \geq G . M . \geq H . M . \\ & \quad \bullet A . M .=G . M .=H . M . \text { if } a_{1}=a_{2}=a_{3}=\ldots=a_{n} \end{aligned}$ |
| Important Results | - $\quad \sum_{r-1}^{n}\left(a_{r} \pm b_{r}\right)=\sum_{r-1}^{n} a_{r} \pm \sum_{r-1}^{n} b_{r}$ |


|  | - $\sum_{r-1}^{n} k a_{r}=k \sum_{r-1}^{n} a_{r}$ <br> - $\sum_{r-1}^{n} k=n k$ where $k$ is constant <br> - $\sum_{r-1}^{n} r=1+2+3+\ldots+n=\frac{n(n+1)}{2}$ <br> - $\sum_{r-1}^{n} r^{2}=1^{2}+2^{2}+3^{2}+\ldots+n^{2}=\frac{n(n+1)(2 n+1)}{6}$ <br> - $\sum_{r-1}^{n} r^{3}=1^{3}+2^{3}+3^{3}+\ldots+n^{3}=\frac{n^{2}(n+1)^{2}}{4}$ |
| :---: | :---: |
| The formula for hyperbola are as stated belo | ola Formula |
| Description | Formula |
| Standard Equation | $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1 \text { where } b^{2}=a^{2}\left(e^{2}-1\right)$ <br> Foci: $S \equiv( \pm a e, 0)$ <br> Directrices: $x= \pm \frac{a}{e}$ <br> Vertices: $A \equiv( \pm a, 0)$ <br> Latus Rectum $l=\frac{2 b^{2}}{a}=2 a\left(e^{2}-1\right)$ |
| Conjugate Hyperbola | $\begin{aligned} & \frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1 \\ & \frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1 \end{aligned}$ <br> Are conjugate hyperbolas of each |
| Auxiliary Circle | $x^{2}+y^{2}=a^{2}$ |
| Parametric Representation | $x=a \sec \sec \theta$ and $y=b \tan \tan \theta$ |
| Position of A point w.r.t hyperbola | $s_{1} \equiv \frac{x_{1}^{2}}{a^{2}}-\frac{y_{1}^{2}}{b^{2}}-1 \geq o r<0$ <br> According to the point $\left(x_{1}, y_{1}\right)$ lies inside on or outside the curve |
| Tangents | Slope form: $y=m x \pm \sqrt{a^{2} m^{2}-b^{2}}$ <br> Point Form: at the point $\left(x_{1}, y_{1}\right)$ is $\frac{x x_{1}}{a^{2}}-\frac{y y_{1}}{b^{2}}=1$ <br> Parametric form: $\frac{x \operatorname{secsec} \theta}{a}-\frac{y \operatorname{tantan} \theta}{b}=1$ |


| Normal: | - At the point $P\left(x_{1}, y_{1}\right)$ is $\frac{a^{2} x}{x_{1}}+\frac{b^{2} y}{y_{1}}=a^{2}+b^{2}=a^{2} e^{2}$ <br> - At the point $P(a \sec \sec \theta, b \tan \tan \theta)$ is $\frac{a x}{\operatorname{secsec} \theta}+\frac{b y}{\operatorname{tantan} \theta}=a^{2}+b^{2}=a^{2} e^{2}$ <br> - Equation of normal in term of its slope $m$ is $y=m x \pm \frac{\left(a^{2}+b^{2}\right) m}{\sqrt{a^{2}-b^{2} m^{2}}}$ |
| :---: | :---: |
| Asymptotes | $\frac{x}{a}+\frac{y}{b}=0 \text { and } \frac{x}{a}-\frac{y}{b}=0$ <br> Pair of asymptotes: $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=0$ |
| Rectangular Or Equilateral Hyperbola | - $x y=c^{2}$ eccentricity is $\sqrt{2}$ <br> - Vertices: $( \pm c \pm c)$ <br> - Foci: $\pm \sqrt{2} c, \pm \sqrt{2} c$ <br> - Directrices: $x+y= \pm \sqrt{2} c$ <br> - Latus Rectum $l=2 \sqrt{2} c=$ T.A. $=C . A$. <br> - Parametric equation $x=c t, y=\frac{c}{t}, t \in R-\{0\}$ <br> - Equation of the tangent at $P\left(x_{1}, y_{1}\right)=\frac{x}{x_{1}}+\frac{y}{y_{1}}=2$ <br> - Equation of the tangent at $P(t)=\frac{x}{t}+t y=2 c$ <br> - Equation of the normal at $P(t)=x t^{3}-y t=c\left(t^{4}-1\right)$ <br> - Chord with a given middle point as $(h, k)=k x+h y=2 h k$ |

## Physics Formulas

## Part 1

## Uniform Circular Motion Formula

The formula for uniform circular motion are as stated below


|  |  |
| :---: | :---: |
| Normal reaction on a convex bridge |  |
| Skidding of vehicle on a level road | $V_{\text {safe }} \leq \sqrt{\mu g r}$ |
| Skidding of an object on a rotating platform | $\omega_{\max }=\sqrt{\frac{\mu g}{r}}$ |
| Bending of Cyclist | $\tan \theta=\frac{v^{2}}{r g}$ |
| Banking of road without friction | $\tan \theta=\frac{v^{2}}{r g}$ |
| Banking of Road with friction | $\frac{V^{2}}{r g}=\frac{\mu+\tan \theta}{1-\mu \tan \theta}$ |
| Maximum also minimum safe speed on a banked frictional road | $V_{\max }=\left[\left(\frac{r g(\mu+\tan \theta)}{1-\mu \tan \theta}\right)\right]^{\frac{1}{2}} V_{\min }=\left[\left(\frac{r g(\tan \theta-\mu)}{1+\mu \tan \theta}\right)\right]^{\frac{1}{2}}$ |

## Alternating Current Formula

The formula for alternating current are as stated below

| Description | Formula |
| :---: | :---: |
| AC and DC current | constant dc <br> periodic dc <br> A current that changes its direction periodically is called alternating current (AC). If a current maintains its direction constant it is called direct current (DC). |


| Root Mean square Value | Root mean square of a function from $t_{1}$ and $t_{2}$ is defined as $f_{r m s}=\sqrt{\frac{t_{2}^{t_{2}} f(t)^{2} d t}{t_{t_{2}}-t_{1}}}$ |
| :---: | :---: |
| Power consumption in AC Circuit | Average power consumed in a cycle $\begin{aligned} & =\frac{1}{T} \int_{0}^{\frac{2 \pi}{\omega}} \frac{P d t}{\frac{2 \pi}{\omega}}=\frac{1}{2} V_{m} I_{m} \cos \phi \\ & \quad=\frac{V_{m}}{\sqrt{2}} \cdot \frac{I_{m}}{\sqrt{2}} \cdot \cos \phi=V_{r m s} I_{r m s} \cos \phi \end{aligned}$ <br> $\cos \phi$ Is known as the Power Factor. |
| Impedance | $z=\frac{V_{m}}{I_{m}}=\frac{V_{r m s}}{I_{r m s}}$ <br> $L$ Is called inductive reactance and is denoted by $X_{L} \frac{1}{\omega C}$ Is called capacitive reactance and is denoted by $X_{c}$. |
| Purely Resistive Circuit | $\begin{gathered} I=\frac{V_{s}}{R}=\frac{V_{m} \sin \omega t}{R}=I_{m} \sin \omega t \\ I_{m}=\frac{V_{m}}{R} \\ I_{r m s}=\frac{V_{r m s}}{R} \\ <p>=V_{r m s} I_{r m s} \cos \phi=\frac{V_{r m s}^{2}}{R} \end{gathered}$ |
| Purely Capacitive Circuit | $\begin{gathered} I=\frac{\frac{V_{m}}{1}}{\omega c} \cos \omega t \\ =\frac{V_{m}}{X_{c}} \cos \omega t=I_{m} \cos \omega t \end{gathered}$ <br> $X_{c}=\frac{1}{\omega C}$ And is called capacitive reactance. |



| Force between two parallel current carrying wires | $\begin{gathered} F_{\frac{A}{B}}=\frac{\mu_{0} I_{A} I_{B}}{(2 \pi r)} \\ I_{A} I_{B}=\text { Current carrying by wires A and B } \end{gathered}$ |
| :---: | :---: |
| The formula for capacitan | Capacitance Formula <br> ce are as stated below |
| Description | Formula |
| Capacitance of a parallel plate capacitor in terms of charge and potential difference | $C=\frac{Q}{V}$ <br> Here, C is the capacitance of the capacitor, Q is the charge stored and V is the potential difference between the plates. |
| Capacitance of a parallel plate capacitor in terms of surface area and distance between the plates | $C=\frac{\varepsilon_{0} A}{d}$ <br> Here, $\varepsilon_{0}$ is the permittivity of free space and its value is <br> $8.854 \times 10^{-12} \mathrm{~m}^{-3} \mathrm{~kg}^{-1} \mathrm{~s}^{4} \mathrm{~A}^{2}, \mathrm{~A}$ is the surface area of the plates and d is the distance between the plates. |
| Capacitance of a spherical capacitor derivation | To find the formula for capacitance of a spherical capacitor we will use the gauss's law. <br> Let the charge on the spherical surface be $Q$, the radius of smaller sphere be $r_{a}$ and radius of the bigger sphere be $r_{b}$. <br> Using gauss's law, we can write: $\begin{aligned} & \oint \vec{E} \cdot d \vec{A}=\frac{Q}{\varepsilon_{0}} \\ & E\left(4 \pi r^{2}\right)=\frac{Q}{\varepsilon_{0}} \\ & E=\frac{Q}{4 \pi \varepsilon_{0} r^{2}} \\ & V=\frac{Q}{4 \pi \varepsilon_{0} r} \end{aligned}$ |
| The potential difference between the plates | $\begin{aligned} V_{a b}=V_{a}-V_{b} & =\frac{Q}{4 \pi \varepsilon_{0}}\left(\frac{1}{r_{a}}-\frac{1}{r_{b}}\right) \\ & =\frac{Q}{4 \pi \varepsilon_{0}} \frac{r_{b}-r_{a}}{r_{a} r_{b}} \end{aligned}$ <br> Therefore, the capacitance will be: $C=\frac{Q}{V_{a b}}=4 \pi \varepsilon_{0} \frac{r_{a} r_{b}}{r_{b}-r_{a}}$ |


| Energy stored in capacitor | - $U=\frac{1}{2} C V^{2}$ <br> - $U=\frac{Q^{2}}{2 C}$ <br> - $U=\frac{Q V}{2}$ <br> Here, U is the energy, C is the capacitance, V is the potential difference and Q is the charge stored. |
| :---: | :---: |
| Energy density of capacitor | Energy density $=\frac{1}{2} \varepsilon_{0} \varepsilon_{r} E^{2}$ <br> In vacuum: <br> Energy density $=\frac{1}{2} \varepsilon_{0} E^{2}$ <br> Here, $\varepsilon_{0}$ is the permittivity of free space, $\varepsilon_{r}$ is the relative permittivity and E is the electric field. |
| Capacitance per unit length of a cylindrical capacitor | Capacitance per unit length $=\frac{2 \pi \varepsilon_{0}}{\ln \left(\frac{b}{a}\right)}$ <br> Here, $\varepsilon_{0}$ is the permittivity of free space, $b$ is the radius of outer cylinder and a is the radius of inner cylinder. |
| Electric field intensity | The formula for electric field intensity between the plates is given as: $E=\frac{\sigma}{\varepsilon_{0}}=\frac{V}{d}$ <br> Here, $\sigma$ is the surface charge density, V is the potential difference and $d$ is the distance between plates. |
| Redistribution of charge when two charged capacitors are connected in parallel | Let us assume a capacitor with capacitance $C_{1}$ with initial charge $Q_{1}$ and capacitor with capacitance $C_{2}$ with initial charge $Q_{2}$. <br> The final charge on capacitor with capacitance $C_{1}$ will be: $Q_{1}^{\prime}=\frac{C_{1}}{C_{1}+C_{2}}\left(Q_{1}+Q_{2}\right)$ <br> final charge on capacitor with capacitance $C_{2}$ will be: $Q_{2}^{\prime}=\frac{C_{2}}{C_{1}+C_{2}}\left(Q_{1}+Q_{2}\right)$ |
| Equivalent capacitance when capacitors are connected in series | $\frac{1}{C_{e q}}=\frac{1}{C_{1}}+\frac{1}{C_{2}}+\frac{1}{C_{3}}+\ldots+\frac{1}{C_{n}}$ <br> Here, $C_{e q}$ is the equivalent capacitance and $C_{1}, C_{2}, C_{3}$ are the capacitance of the capacitors. |


| Equivalent <br> capacitance of the <br> capacitors <br> connected in <br> parallel | $C_{e q}=C_{1}+C_{2}+C_{3}+\ldots C_{n}$ |
| :--- | :--- |
| Charging of <br> capacitor | $q=q_{0}\left(1-e^{-\frac{t}{\tau}}\right)$ <br> Here, $q$ is the charge on the capacitor at time $\mathrm{t}, \tau$ is the time <br> constant and $q_{0}$ is the charge on the capacitor at steady state. |
| Discharging of <br> capacitor | $q=q_{0} e^{-\frac{t}{\tau}}$ <br> Here, q is the charge on the capacitor at time $\mathrm{t}, \tau$ is the time <br> constant and $q_{0}$ is the charge on the capacitor at steady state. |

## Part 2

## Centre of Mass Formula

The formula for centre of mass are as stated below

| Description | Formula |
| :---: | :---: |
| Centre of mass of a system with $n$ number of masses situated on a line at different positions | The centre of mass of the system will be: $\vec{r}_{c m}=\frac{\left(m_{1} \vec{r}_{1}+m_{2} \vec{r}_{2}+m_{3} \vec{r}_{3}+\ldots+m_{n} \vec{r}_{n}\right)}{m_{1}+m_{2}+m_{3}+\ldots+m_{n}}$ <br> here, $m_{1}, m_{2}, m_{3}$ are the masses situated at $\vec{r}_{1}, \vec{r}_{2}, \vec{r}_{3}$ respectively. |
| Centre of mass of a system with $n$ number of masses situated on a 2D plane | Let the masses $m_{1}, m_{2}, m_{3}, m_{n}$ be placed at coordinates $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right),\left(x_{3}, y_{3}\right),\left(x_{n}, y_{n}\right)$ <br> So, we will find the centre of mass for x and y axis respectively using the formula: $\begin{aligned} & r_{x}=\frac{m_{1} x_{1}+m_{2} x_{2}+m_{3} x_{3}+\ldots+m_{n} x_{n}}{m_{1}+m_{2}+m_{3}+\ldots+m_{n}} \\ & r_{y}=\frac{m_{1} y_{1}+m_{2} y_{2}+m_{3} y_{3}+\ldots+m_{n} y_{n}}{m_{1}+m_{2}+m_{3}+\ldots+m_{n}} \end{aligned}$ |


|  | The centre of mass of the system will be: $\left(r_{x^{\prime}} r_{y}\right)$. |
| :---: | :---: |
| Centre of mass of a rectangular plate | The centre of mass of a uniform rectangular plate of length $L$ and breadth $B$ is given as: $\begin{aligned} & r_{x}=\frac{B}{2} \\ & r_{y}=\frac{L}{2} \end{aligned}$ |
| Centre of mass of a triangular plate | The centre of mass of a uniform triangular plate is given by the formula: $r_{c}=\frac{h}{3}$ <br> Where, h is the height of the plate. |
| Centre of mass of a semi-circular ring | The centre of mass of a semi-circular ring is given as: $\begin{aligned} & r_{y}=\frac{2 R}{\pi} \\ & r_{x}=O \end{aligned}$ <br> Here, R is the radius of the semi- Circle. |
| Centre of mass of a semi-circular disc | The centre of mass of a semi-circular disc is given as: $\begin{aligned} & r_{y}=\frac{4 R}{3 \pi} \\ & r_{x}=0 \end{aligned}$ <br> Here, R is the radius of the semi- Circle. |
| Centre of mass of a hemispherical shell | The centre of mass of a hemispherical shell is given as: $\begin{aligned} & r_{y}=\frac{R}{2} \\ & r_{x}=0 \end{aligned}$ <br> Here, R is the radius of the semi- Circle. |
| Centre of mass of a solid hemisphere | The centre of mass of a solid hemisphere is given as: $\begin{aligned} & r_{y}=\frac{3 R}{8} \\ & r_{x}=0 \end{aligned}$ <br> Here, R is the radius of the hemisphere. |
| Centre of mass of a circular cone | The centre of mass of a circular cone is given as: $r_{y}=\frac{h}{4}$ <br> Here, $h$ is the height of the cone. |


| Centre of mass of a hollow circular cone | The centre of mass of a hollow circular cone is given as: $r_{y}=\frac{h}{3}$ <br> Here, h is the height of the cone. |
| :---: | :---: |
| The formula for circula | Circular Motion <br> motion are as stated below |
| Description | Formula |
| Average angular velocity | $\omega_{\text {average }}=\frac{\theta_{2}-\theta_{1}}{t_{2}-t_{1}}$ <br> Here, $\theta_{2}$ is the angle at time $t_{1}$, and $\theta_{1}$ is the angle at time $t_{1}$. |
| Average angular acceleration | $\alpha_{a v}=\frac{\omega_{2}-\omega_{1}}{t_{2}-t_{1}}$ <br> Here, $\omega_{2}$ is the angular frequency at time $t_{2}$ and $\omega_{1}$ is the angular frequency at time $t_{1}$. |
| Tangential acceleration | $a_{t}=\frac{d V}{d t}$ <br> Here $d V$ is the change in velocity over time $d t$. $a_{t}=r \frac{d \omega}{d t}$ <br> Here, $r$ is the radius, $d \omega$ is the change in angular frequency over time $d t$. |
| Centripetal acceleration | $\begin{aligned} & a_{c}=\frac{v^{2}}{r} \\ & \text { or } a_{c}=\omega^{2} r \end{aligned}$ <br> Here, $v$ is the linear velocity, $r$ is the radius and $\omega$ is the angular frequency. |
| Normal reaction on a body moving on a concave bridge | $N=m g \cos \cos \theta+\frac{m v^{2}}{r}$ <br> Here, m is the mass, g is the gravitational acceleration, $\theta$ is the angle, $v$ is the linear velocity and $r$ is the radius of the bridge. |
| Normal reaction on a convex bridge | $N=m g \cos \cos \theta-\frac{m v^{2}}{r}$ <br> Here, $m$ is the mass, $g$ is the gravitational acceleration, $\theta$ is the angle, $v$ is the linear velocity and $r$ is the radius. |
| Safe velocity of a vehicle on a level road | $v_{\text {safe }} \leq \sqrt{\mu g r}$ <br> Here, $v_{\text {safe }}$ is the safe velocity, $\mu$ is the coefficient of friction, g is the gravitational acceleration and $r$ is the radius. |


| Banking angle | $\tan \theta=\frac{v^{2}}{r g}$ <br> Here, $\theta$ is the banking angle, $v$ is the linear velocity, $r$ is the radius of the curve and $g$ is the gravitational acceleration. |
| :---: | :---: |
| Centrifugal force | $f=m \omega^{2} r$ <br> Here, f is the centrifugal force, m is the mass, $\omega$ is the angular velocity and $r$ is the radius. |
| Conical pendulum | $T=2 \pi \sqrt{\frac{L \cos \theta}{g}}$ <br> Here, $L$ is the length of the pendulum, $\theta$ is the angle made by the string with the vertical and $g$ is the gravitational acceleration. |
| The formula for de bro | De Broglie Wavelength Formula <br> glie wavelength are as stated below |
| Description | Formula |
| De Broglie wavelength | $\begin{aligned} & \lambda=\frac{h}{m v} \\ & \text { Or } \lambda=\frac{h}{\sqrt{2 m K E}} \end{aligned}$ <br> Here, $\lambda$ is the de Broglie wavelength, $h$ is the Plank's constant, $m$ is the mass, $v$ is the velocity, KE is the kinetic energy. |
| Radius of electron in hydrogen like atoms | $r_{n}=\frac{n^{2}}{Z} a_{0}$ <br> Here, $r_{n}$ is the radius of $\mathrm{n}^{\text {th }}$ orbit, $a_{0}$ is a constant whose value is $0.529 \times 10^{-10} \mathrm{~m}$ and z is the atomic number. |
| Speed of electron in hydrogen like atoms | $v_{n}=\frac{Z}{n} v_{0}$ <br> Here, Z is the atomic number, n is the orbit and $v_{0}$ is a constant whose value is $\text { 2. } 19 \times 10^{6} \mathrm{~m} / \mathrm{s} \text {. }$ |
| Energy in $\mathrm{n}^{\text {th }}$ orbit | $E_{n}=E_{1} \cdot \frac{z^{2}}{n^{2}}$ <br> Here, $E_{n}$ is energy of the $\mathrm{n}^{\text {th }}$ orbit, $E_{1}$ is the energy of the $1^{\text {st }}$ orbit and its value is $-13.6 \mathrm{eV}, Z$ is the atomic number and n is the number orbit. |
| Wavelength corresponding to spectral lines | $\frac{1}{\lambda}=R\left[\frac{1}{n_{1}^{2}}-\frac{1}{n_{2}^{2}}\right]$ <br> Here, $\lambda$ is the wavelength, $R$ is the Rydberg constant and its value is $1.097 \times 10^{7} \mathrm{~m}^{-1}$ <br> Values of n for different series. <br> Lyman series: $n_{1}=1 ; n_{2}=2,3,4, \ldots$ <br> Balmer series: $n_{1}=2 ; n_{2}=3,4,5, \ldots$ |


|  | Paschim series: $n_{1}=3 ; n_{2}=4,5,6, \ldots$ |
| :--- | :--- |
| Minimum <br> wavelength for $\mathbf{x}$ <br> rays | $\lambda_{\text {min }}=\frac{h c}{e V_{0}}$ <br> Or $\lambda_{\text {min }}=\frac{12400}{V_{0}} \times 10^{-10} m$ <br> here, $\lambda_{\text {min }}$ is the minimum wavelength, h is the plank's constant, c is the speed <br> of light, e is the charge of an electron and $V_{0}$ is the accelerating voltage. |
| Radius of nucleus | $R=R_{0} A^{1 / 3}$ <br> Here, R is the radius of the atom, $R_{0}$ is a constant whose value is $1.1 \times 10^{-15} m$ <br> , A is the mass number of the atom. |
| Number of nuclei <br> during a radioactive <br> decay | $N=N_{0} e^{-\lambda t}$ <br> here, $\mathrm{N}^{2}$ is the number of nuclei at time $\mathrm{t}, N_{0}$ is the initial number of nucleus <br> and $\lambda_{\text {is the decay constant. }}$ |
| Half-life of a <br> radioactive sample | $T_{1 / 2}=\frac{0.693}{\lambda}$ <br> Here, $T_{1 / 2}$ is the half-life period and $\lambda$ is the decay constant. |
| Average life | $T_{a v}=\frac{T_{\frac{1}{2}}^{2}}{0.693}$ <br> here, $T_{a v}$ is the average life and $T_{1 / 2}$ is the half- life period. |

## Part 3

## Current Electricity

The formula for current electricity are as stated below

| Description | $\quad$ Formula |
| :--- | :--- |
| Formula for current | • $I=\frac{\Delta q}{\Delta t}$ <br>  <br>  <br>  <br>  <br>  <br> Here, $I q=\frac{\Delta q}{\Delta t}=\frac{d q}{d t}$ <br> the time in which the flown through the circuit and $\Delta t$ is |
| Electric current in a flown. <br> conductor(wire) | $I=n A e V_{d}$ <br> $v_{d}=\frac{\lambda}{\tau}$ |


|  | Here, n is the number of free electrons, A is the area of conductor, e is the charge of an electron, $V_{d}$ is the drift velocity, $\lambda$ is the linear charge density and $\tau$ is the relaxation time. |
| :---: | :---: |
| Potential difference using ohm's law | $V=I R$ <br> Here, V is the potential difference, I is the current flowing through the conductor and $R$ is the resistance offered by the conductor. |
| Resistance in terms of resistivity | $R=\frac{\rho l}{A}$ <br> Here, $\rho$ is the resistivity of the material of the conductor, I is the length of the conductor and $A$ is the area of cross section of the conductor. |
| Change in resistance due to temperature | $R=R_{0}(1+\alpha \Delta T)$ <br> Here, R is the resistance, $R_{0}$ is the initial temperature, $\alpha$ is the temperature coefficient of the resistivity and $\Delta T$ is the change in temperature. |
| Electric power | $P=V I$ <br> Here, P is the power, V is the potential difference and I is the current. <br> Also, $\begin{aligned} & P=I^{2} R \\ & P=\frac{V^{2}}{R} \end{aligned}$ |
| Heat energy released due to current | $H=V I t$ <br> also $\begin{aligned} & H=I^{2} R t \\ & H=\frac{V^{2}}{R} t \end{aligned}$ <br> Here, H is the heat released in joules, V is the potential difference, R is the resistance, l is the current and t is the total time the current was flowing through the conductor. |
| Equivalent resistance when resistors are connected in series | $R_{e q}=R_{1}+R_{2}+R_{3}+\ldots+R_{n}$ <br> Here, $R_{e q}$ is the equivalent resistance, $R_{1}, R_{2}, R_{3}$ are the resistance of the resistors. |
| Equivalent resistance when | $\frac{1}{R_{e q}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\frac{1}{R_{3}}+\ldots+\frac{1}{R_{n}}$ |


| resistors are connected in parallel |  |
| :---: | :---: |
| Potential difference when cells are connected in parallel | $E_{e q}=\frac{\left(\frac{\varepsilon_{1}}{r_{1}}+\frac{\varepsilon_{2}}{r_{2}}+\frac{\varepsilon_{3}}{r_{3}}+\ldots+\frac{\varepsilon_{n}}{r_{n}}\right)}{\frac{1}{r_{1}}+\frac{1}{r_{2}}+\frac{1}{r_{3}}+\ldots+\frac{1}{r_{n}}}$ <br> Here, $\varepsilon_{1}, \varepsilon_{2}, \varepsilon_{3}$ are the emf of the cells and $r_{1}, r_{2}, r_{3}$ are the internal resistance of the cells. |
| Ammeter using galvanometer | To measure the maximum current I using a galvanometer, we need to connect a shunt resistance in parallel with the galvanometer. <br> The value of the resistance is calculated as: $S=\frac{I_{g} R_{g}}{I}$ <br> Here, S is the value of shunt resistance, $I_{g}$ is the current through galvanometer, $R_{g}$ is the resistance of the galvanometer and $I$ is the maximum current to be measured. |
| Voltmeter using galvanometer | To measure a potential difference using a galvanometer, we need to connect a series resistance with it. The value of the resistance that needs to be connected is: $R_{s}=\frac{V}{I_{g}}-R_{g}$ <br> Here, V is the maximum potential difference to be measured, $I_{g}$ is the current through galvanometer and $R_{g}$ is the resistance of the galvanometer. |
| Electric Current Formula <br> The formula for electric current are as stated below |  |
| Description | Formula |
| Electric current | $\begin{aligned} & I=q / t=n e / t \\ & \text { Where } I=\text { strength of current; } q \text {-charge; } \mathrm{t} \text { - time } \end{aligned}$ |
| Resistance | $R=\frac{V}{i}$ and <br> Conductance $G=\frac{I}{R}$ <br> Where <br> $V$ - potential difference, |


|  | $\begin{aligned} & i-\text { current, } \\ & R=\frac{\rho l}{A}=\frac{\rho l}{\pi r^{2}} \end{aligned}$ <br> Where, $R$ - Resistance fo the wire; <br> $\rho$ - Resistivity, <br> $l$ - length of the wire, <br> A - area of cross section of the wire |
| :---: | :---: |
| Variation of resistance with the temperature | $\begin{aligned} & R_{T}=R_{\mathrm{o}}[1+\alpha(t)] \\ & \rightarrow \alpha=\frac{R_{t}-R_{o}}{R_{\mathrm{o}}(t)} l^{\circ} \mathrm{C} \\ & \alpha=\frac{\left(R_{1}-R_{2}\right)}{R_{1}\left(t_{2}-t_{1}\right)} l^{\circ} \mathrm{C} \end{aligned}$ <br> Here, <br> $\mathrm{R}=$ resistance at temperature $t^{\circ} \mathrm{C}$ <br> $R_{\mathrm{o}}=$ resistance at temperature $0^{\circ} \mathrm{C}$ <br> $\alpha=$ temperature coefficient of resistance |
| Conductivity | Reciprocal of resistivity. $\sigma=\frac{1}{\rho}$ <br> Where $-\sigma$-conductivity, $\rho$-resistivity |
| Terminal voltage | Case-1: When battery is delivering current $V=E-\text { ir or } i=\frac{E}{R+r}$ <br> Where <br> $V$-terminal P.d, $E$ - emf of the cell, $r$-internal resistance of the cell, $R-$ external resistance. <br> Case 2: when battery is charging $V=E+i r$ |
| Kirchhoff's laws | Kirchhoff's First laws: <br> $\sum i=0$ at any junction. <br> Kirchhoff's second law: <br> $\sum i R=0$ in a closed circuit. |
| Metre Bridge | 1. $\frac{x}{R}=\frac{l_{1}}{l_{2}} \Rightarrow \frac{x}{R}=\frac{l_{1}}{\left(100-l_{1}\right)}$ <br> Where $x$ - unknown resistance of given wire, R -resistance in the resistance box, $l_{1}$-balancing length from left end of the bridge to Jockey. <br> 2. $\rho=\frac{x A}{l}=x \frac{\pi r^{2}}{l}$ <br> Where $\rho$-Resistivity of the wire, $x$-resistance of wire, <br> A - area of cross section of the wire, <br> $l$-length of the wire. |
| Potentio Meter | Emf of cell in the secondary circuit $E_{s}=I \rho l$ |


|  | 1. Comparison of emf's of two cells: $\frac{E_{1}}{E_{2}}=\frac{l_{1}}{l_{2}}$ Where $E_{1}$ and $E_{2}$-emf of the first and second cell, $l_{1}$ and $l_{2}$-the balancing lengths of individual cells respectively. <br> 2. $r=\frac{R\left(l_{1}-l_{2}\right)}{l_{2}}$ |
| :---: | :---: |
| The formula for electrom | ectromagnetic Induction Formula <br> netic induction are as stated below |
| Description | Formula |
| Magnetic Flux | The magnetic flux through a plane of area $d A$ placed in a uniform magnetic field $B$ is given as $\phi=\int \vec{B} \cdot d \vec{A}$ <br> When the surface is closed, then magnetic flux will be zero. This is due to magnetic lines of force are closed lines and free magnetic poles is not exist |
| Electromagnetic Induction: Faraday's Law | First Law: Whenever magnetic flux linked with a circuit changes with time, an induced emf is generated in the circuit that lasts as long as the change in magnetic flux continues. <br> Second Law: According to this law, the induced emf is equal to the negative rate of change of flux through the circuit. $E=-\frac{d \phi}{d t}$ |
| Lenz's Law | The direction of induced emf or current in the circuit is in such a way that it opposes the cause due to which it is produced. Therefore, $E=-N\left(\frac{d \phi}{d t}\right)$ |
| Induced emf | Induced emf is given as $\begin{gathered} E=-N\left(\frac{d \phi}{d t}\right) \\ E=-N\left(\frac{\phi_{1}-\phi_{2}}{t}\right) \end{gathered}$ |
| Induced Current | Induced Current is given as $I=\frac{E}{R}=\frac{N}{R}\left(\frac{d \phi}{d t}\right)=\frac{N}{R}\left(\frac{\phi_{1}-\phi_{2}}{t}\right)$ |
| Self - Induction | Change in the strength of flow of current is opposed by a characteristic of a coil is known as self-inductance. <br> It is given as $\phi=L I$ <br> Here, $L=$ coefficient of self - inductance <br> Magnetic flux rate of change in the coil is given as $\frac{d \Phi}{d t}=L \frac{d l}{d t}=-E$ |
| Mutual - Induction | Mutual - Induction is given as $e_{2}=\frac{d\left(N_{2} \phi_{2}\right.}{d t}=M \frac{d l_{1}}{d t}$ |


|  | Therefore, | $M=\frac{\mu_{0} N_{1} N_{2} A}{l}$ |
| :--- | :--- | :--- |

## Part 4

## Electromagnetic Induction Formula

The formula for electromagnetic induction are as stated below

| Description | Formula |
| :---: | :---: |
| Magnetic Flux | The magnetic flux through a plane of area $d A$ placed in a uniform magnetic field B is given as $\phi=\int \vec{B} \cdot d \vec{A}$ <br> When the surface is closed, then magnetic flux will be zero. This is due to magnetic lines of force are closed lines and free magnetic poles is not exist |
| Electromagnetic Induction: Faraday's Law | First Law: Whenever magnetic flux linked with a circuit changes with time, an induced emf is generated in the circuit that lasts as long as the change in magnetic flux continues. <br> Second Law: According to this law, the induced emf is equal to the negative rate of change of flux through the circuit. $E=-\frac{d \phi}{d t}$ |
| Lenz's Law | The direction of induced emf or current in the circuit is in such a way that it opposes the cause due to which it is produced. Therefore, $E=-N\left(\frac{d \phi}{d t}\right)$ |
| Induced emf | Induced emf is given as $\begin{gathered} E=-N\left(\frac{d \phi}{d t}\right) \\ E=-N\left(\frac{\phi_{1}-\phi_{2}}{t}\right) \end{gathered}$ |
| Induced Current | Induced Current is given as $I=\frac{E}{R}=\frac{N}{R}\left(\frac{d \phi}{d t}\right)=\frac{N}{R}\left(\frac{\phi_{1}-\phi_{2}}{t}\right)$ |
| Self - Induction | Change in the strength of flow of current is opposed by a characteristic of a coil is known as self-inductance. <br> It is given as $\phi=L I$ <br> Here, $L=$ coefficient of self - inductance <br> Magnetic flux rate of change in the coil is given as $\frac{d \phi}{d t}=L \frac{d l}{d t}=-E$ |
| Mutual - Induction | Mutual - Induction is given as $e_{2}=\frac{d\left(N_{2} \phi_{2}\right)}{d t}=M \frac{d l_{1}}{d t}$ |


|  | Therefore, $M=\frac{\mu_{0} N_{1} N_{2} A}{l}$ |
| :---: | :---: |
| The formula for electroma | Electromagnetic Waves <br> netic waves are as stated below |
| Description | Formula |
| Gauss's law for electricity | $\oint E \cdot d A=\frac{Q}{\varepsilon_{0}}$ <br> Here, E is the electric field, A is the area, Q is the charge and $\varepsilon_{0}$ is the permittivity of free space. |
| Gauss's law for magnetism | $\oint B \cdot d A=0$ <br> $B$ is the magnetic field and A is the area. |
| Faraday's law | $\oint E \cdot d l=-\frac{d \Phi_{B}}{d t}$ <br> Here, E is the electric field, I is the length of the conductor, $\Phi_{B}$ is the magnetic flux and t is the time. |
| Ampere- Maxwell law | $\oint B \cdot d l=\mu_{0} i+\mu_{0} \varepsilon_{0} \frac{d \Phi_{B}}{d t}$ <br> Here, $B$ is the magnetic field, $I$ is the length of the conductor, $\mu_{0}$ is permeability of free space, $i$ is the current flowing through the conductor, $\varepsilon_{0}$ is the permittivity of free space, $\Phi_{B}$ is the magnetic flux and t is the time. |
| Speed of light in vacuum | $c=1 / \sqrt{\mu_{0} \varepsilon_{0}}$ |
| The formula for electrosta | Electrostatics Formula <br> istics are as stated below |
| Description | Formula |
| Electrostatic force between two-point charges | $\vec{F}=\frac{1}{4 \pi \varepsilon_{0}} \frac{q_{1} q_{2}}{\|\vec{r}\|^{2}} \hat{r}$ |


|  | Here, $\varepsilon_{0}$ is the permittivity of free space, $q_{1} q_{2}$ are the point charges and $r$ is the distance between the charges. |
| :---: | :---: |
| Electric field | $\vec{E}=\frac{\vec{F}}{q_{0}}$ <br> Here, $\vec{F}$ is the electrostatic force experienced by test charge $q_{0}$. |
| Electric field due to a uniformly charged ring | $E_{a x i s}=\frac{K Q x}{\left(R^{2}+x^{2}\right)^{\frac{3}{2}}}$ <br> Here, K is the relative permeability, Q is the charge on the ring, x is the perpendicular distance from the ring to the point at which the electric field is to be calculated and $R$ is the radius of the ring. |
| Electric field due to a uniformly charged disc | $E=\frac{\sigma}{2 \varepsilon_{0}}\left[1-\frac{x}{\sqrt{R^{2}+x^{2}}}\right]$ <br> Here, $\sigma$ is the surface charge density, $\varepsilon$ is the permittivity of free space, x is the perpendicular distance from the centre of the disk and R is the radius of the disk. |
| Work done by external force | The work done by an external force in bringing a charge q from potential $V_{B}$ to $V_{A}$ is: $W=q\left(V_{A}-V_{B}\right)$ |
| Electrostatic potential energy | $U=q V$ <br> Here, q is the charge and V is the potential. |
| Electrostatic energy | $U=\frac{1}{4 \pi \varepsilon_{0}} \frac{q_{1} q_{2}}{r}$ <br> here $q_{1} q_{2}$ are the charges and $r$ is the distance between the charges. |
| Electric potential at a point due to a point charge | $V=\frac{1}{4 \pi \varepsilon_{0}} \frac{q}{r}$ |
| Dipole moment | The formula for calculating electric dipole moment is $\vec{p}=q \vec{d}$ <br> Here q is the magnitude of the charge and d is the distance between the charges. |
| Potential at a point due to dipole | The potential at a point due to a dipole is given as: $V=\frac{1}{4 \pi \varepsilon_{0}} \frac{p \cos \theta}{r^{2}}$ <br> Here, p is the dipole moment and $\theta$ is the angle made by the line joining the point and the centre of the dipole with the line joining the charges and $r$ is the distance from the point at which the potential is to be calculated and the line joining the charges. |
| Torque experienced by dipole due to electric field | $\vec{\tau}=\vec{p} \times \vec{E}$ <br> here, $\vec{p}$ is the dipole moment and $\vec{E}$ is the electric field. |

## Friction Formula

The formula for friction are as stated below

| Description | Formula |
| :--- | :--- |
| Force due to kinetic |  |
| friction | The formula for calculating the force due to kinetic friction is: <br> $F_{k}=\mu_{k} R$ <br> here $F_{k}$ is the force due to kinetic friction, $\mu_{k}$ is the coefficient <br> of kinetic friction and R is the normal reaction force on the <br> body on which the force is acting. <br> If the body is lying on levelled plane, then the normal force is <br> given as: <br> $R=m g$ <br> Here m is the mass and g is the gravitational acceleration. <br> When the body is lying on a plane that is at some angle $\theta$ with <br> the horizontal then the normal reaction force on the body is <br> given as: |
| Force due to static <br> friction | The formula for calculating the force due to static friction is: <br> $F_{s}=\mu_{s} R$ <br> here, $F_{s}$ is the force due to static friction, $\mu_{s}$ is the coefficient <br> of static friction and R is the normal reaction force on the <br> body. |

## Part 5

|  | Linear Momentum Formula |
| :---: | :---: |
| The formula for linear momentum are as stated below |  |
| Description | Formula |
| Linear Momentum | $p=m v$ <br> $p$ is linear momentum, $m$ is mass and $v$ is velocity |


| Conservation of <br> momentum | $m_{1} u_{1}+m_{2} u_{2}=m_{1} v_{1}+m_{2} v_{2}$ <br> Where <br> $\mathrm{P}=$ Momentum, <br> $\mathrm{m}=$ Mass and <br> $\mathrm{u}, \mathrm{v}=$ velocity |
| :--- | :--- |
| Elastic Collision | $m_{1} v_{1 i}+m_{2} v_{2 i}=m_{1} v_{1 f}+m_{2} v_{2 f}$ <br> Where $\mathrm{i}=$ initial and $\mathrm{f}=$ final |
| Inelastic collision | $m_{1} v_{1 i}+m_{2} v_{2 i}=\left(m_{1}+m_{2}\right) v_{2 f}$ |
| Force (from Newton's <br> second law) | $F=m \times a$ <br> $F_{n e t}=\frac{d p}{d t}$ |
| Momentum in terms of <br> kinetic energy | $p=m v$ <br> $p^{2}=m^{2} v^{2}$ <br> $p^{2}=2 m\left(\frac{1}{2} m v^{2}\right)$ <br> $p^{2}=2 m K$ <br> Here, $\mathrm{K}=$ kinetic energy |
| Dimensional Formula of <br> Momentum | $\left[M^{1} L^{1} T^{-1}\right]$ |

## Geometrical Optics Formula

The formula for geometrical optics are as stated below

| Description | Formula |
| :---: | :---: |
| Laws of Reflection of light | The incident ray, refracted ray, and normal always lie on the same plane. <br> Snell's law <br> According to the Snell's law $\frac{\sin i}{\sin r}=\text { constant }$ <br> Here, <br> $i=$ angle of incidence <br> $r=$ angle of reflection |
| Relative refractive index | The Relative refractive index is given as $n=\frac{c}{v}$ <br> here, <br> $\mathrm{n}=$ refractive index <br> $c=$ speed of light in vacuum <br> $\mathrm{v}=$ speed of light in medium |


| Lateral Shift | Lateral Shift is given as $\text { lateral shift }=t \frac{\sin (i-r)}{\cos r}$ |
| :---: | :---: |
| Normal shift on a surface | The normal shift on a single surface is given as $\text { Normal shift }=t\left(1-\frac{1}{n}\right)$ |
| Relation between refractive index and critical angle | The relation between refractive index and critical angle is given as $n=\frac{1}{\sin c}$ |
| Refraction throug prism | The refractive index of a prism is given as $n=\frac{\sin \left(a+\frac{\delta}{2}\right)}{\sin \frac{A}{2}}$ |
| Lens maker formu thin lenses | Lens maker formula for thin lenses is given as $\frac{1}{f}=(n-1)\left[\frac{1}{R_{1}}-\frac{1}{R_{2}}\right]$ |
| Power of lens | Power of lens is given as $P=\frac{1}{f}$ |
| Equivalent focal le of combination of thin lenses | $\frac{1}{f}=\frac{1}{f_{1}}+\frac{1}{f_{2}}$ |
| The formula for heat | eat And Thermodynamics Formula <br> hermodynamics are as stated below |
| Description | Formula |
| Kirchhoff's Law | $\frac{\text { Emissive power of body }}{\text { Absorptive power of body }}=\text { Emissive power of black body }$ |


| Conduction | Rate of flow of heat in conduction is determined as $\frac{d Q}{d t}=-K A \frac{d T}{d x}$ <br> - $\mathrm{K}=$ thermal conductivity <br> - $A=$ area of cross-section <br> - $\mathrm{dx}=$ thickness <br> - $\mathrm{dT}=$ temperature difference |
| :---: | :---: |
| Newton's law of cooling | $\frac{d \theta}{d t}=\left(\theta-\theta_{0}\right)$ <br> - Here, <br> - $\theta$ and $\theta_{0}=$ temperature corresponding to object and surroundings. |
| Temperature scales | $\begin{gathered} F=32+\frac{9}{5} \times C \\ K=C+273.16 \end{gathered}$ <br> - $F=$ Fahrenheit scale <br> - $\mathrm{C}=$ Celsius scale <br> - $K=$ Kelvin scale |
| Ideal Gas equation | $P V=n R T$ <br> - Here, <br> - $n=$ number of moles <br> - $\mathrm{P}=$ pressure <br> - $V=$ Volume <br> - $\mathrm{T}=$ Temperature |
| Van der Waals equation | $\left(p+a\left(\frac{n}{V}\right)^{2}\right)(V-n b)=n R T$ <br> - $a\left(\frac{n}{V}\right)^{2}=$ correction factor for intermolecular forces <br> - $\mathrm{nb}=$ correction factor for molecule size <br> - $\mathrm{n}=$ number of moles <br> - $\mathrm{T}=$ Temperature <br> - $\mathrm{V}=$ Volume <br> - $p=$ pressure |
| Thermal expansion | Linear Expansion $L=L_{0}(1+\alpha \Delta T)$ |


|  | Area Expansion <br> Volume Expansion | $\begin{aligned} & A=A_{0}(1+\beta \Delta T) \\ & V=V(1+\gamma \Delta T) \end{aligned}$ |
| :---: | :---: | :---: |
| Relation between $\alpha, \beta$ and $y$ for the isotropic solid |  | $\frac{\alpha}{1}=\frac{\beta}{2}=\frac{\gamma}{3}$ |
| Stefan- <br> Boltzmann's <br> law | $u=\sigma A T^{4}$ (Perfect $u=e \sigma A T^{4}$ (Notap <br> - here, <br> - $\sigma=$ Stefan's co <br> - $\frac{u}{A}=$ energy flu <br> - $e=$ emissivity | ack body) <br> fect black body) $\text { stant }=5.67 \times 10^{-8} \text { watt } / \mathrm{m}^{2} \mathrm{~K}^{4}$ |
| Thermal resistance to conduction | Thermal resistance is give <br> - $\mathrm{K}=$ material's <br> - L = plane thick <br> - A = plane area | $R=\frac{L}{K A}$ <br> nductivity <br> ss |
| Hooke's Law Formula <br> The formula for Hooke's law are as stated below |  |  |
| D Description |  | Formula |
| Formula for Hooke's Law |  | $F=-k x$ <br> Where $\mathrm{F}=$ force, $\mathrm{k}=$ constant and $\mathrm{x}=$ displacement Note: Hooke's law can be expressed in the form of stress and strain. |
| According to Hooke's law |  | Stress $\propto$ Strain <br> That is, <br> Stress $=K \times$ Strain <br> Where K is the proportionality constant |
| Formula for Stress |  | $\text { Stress }(\sigma)=F / A$ <br> Where, |



|  | $\phi=\int \vec{B} \cdot d \vec{A}$ <br> When the surface is closed, then magnetic flux <br> will be zero. This is due to magnetic lines of force <br> are closed lines and free magnetic poles is not <br> exist |
| :--- | :--- |
| Induced Current | Induced Current is given as <br> $I=\frac{E}{R}=\frac{N}{R}\left(\frac{d \phi}{d t}\right)=\frac{N}{R}\left(\frac{\phi_{1}-\phi_{2}}{t}\right)$ |
| Mutual - Induction | Mutual - Induction is given as <br> $e_{2}=\frac{d\left(N_{2} \phi_{2}\right.}{d t}=M \frac{d l_{1}}{d t}$ <br> Therefore, $\quad M=\frac{\mu_{0} N_{1} N_{2} A}{l}$ |

## Part 6

## Faraday's Law Formula

The formula for Faraday's law are as stated below

| Description | Formula |
| :---: | :---: |
| Faraday's first law | The first law of Faraday's electromagnetic induction explains that when a wire is kept in a field that experiences a constant change in its magnetic field, then an electromagnetic field is developed. This phenomenon of development of the electromagnetic field is called an induced emf. |
| Faraday's second law | 1. It states that the emf induced in a conductor is equivalent to the rate at which the flux is linked to the circuit changes. $\varepsilon=-d \phi / d t$ <br> Where, $\varepsilon=$ the emf or electromotive force $\phi=\text { the magnetic flux }$ <br> 2. If there are N number of turns in the coil then the total magnetic induction in a coil is represented as |


|  | $\varepsilon=-N d \phi / d t$ |
| :---: | :---: |
| Magnetic flux | It is the integral (sum) of all of the magnetic fields passing through infinitesimal area elements $d A$. $\Phi_{B}=\int \vec{B} \cdot d \vec{A}$ |
| The magnetic flux through a surface | The component of the magnetic field passing through that surface. The magnetic flux through some surface is proportional to the number of field lines passing through that surface. The magnetic flux passing through a surface of vector area $A$ is $\Phi_{B}=B \cdot A=B A \cos \theta$ |
| Lenz's Law | The direction of induced emf or current in the circuit is in such a way that it opposes the cause due to which it is produced. Therefore, $E=-N\left(\frac{d \phi}{d t}\right)$ |
| Induced emf | Induced emf is given as $\begin{gathered} E=-N\left(\frac{d \phi}{d t}\right) \\ E=-N\left(\frac{\phi_{1}-\phi_{2}}{t}\right) \end{gathered}$ |
| Magnetic Flux | The magnetic flux through a plane of area $d A$ placed in a uniform magnetic field $B$ is given as $\phi=\int \vec{B} \cdot d \vec{A}$ |
| Fluid mechanics \& Properties of Matter Formula <br> The formula for fluid mechanics and properties of matter are as stated below |  |
| Description | Formula |
| Pressure | $P=\frac{F}{A}$ <br> For hydraulic press: $F=\frac{A}{a} f$ <br> Here, P is the pressure, F is the force applied on bigger piston with area $A$ and $f$ is the force on the smaller piston with area a. |
| Angle made by liquid surface when the container experiences an acceleration | $\tan \theta=\frac{a_{0}}{g}$ <br> here, $\theta$ is the angle made by the liquid surface with the horizontal, $a_{0}$ is the acceleration of the container and $g$ is the gravitational acceleration. |
| Continuity equation | According to the equation of continuity, the product of velocity and the area of cross section at any section in a tube is constant. |


|  | $a_{1} v_{1}=a_{2} v_{2}$ <br> here, $a_{1} v_{1}$ are the area of cross section and velocity of fluid at section 1 and $a_{2} v_{2}$ are the area of cross section and velocity of the fluid at section 2. |
| :---: | :---: |
| Bernoulli's equation | According to Bernoulli's equation the total energy of liquid flowing through a tube is constant throughout the tube. $\frac{P}{\rho g}+\frac{v^{2}}{2 g}+Z=\text { constant }$ <br> Here, $P$ is the pressure, $\rho$ is the density of the fluid, $g$ is the gravitational acceleration, $v$ is the velocity of the fluid and $Z$ is the potential head. <br> The term $\left(\frac{P}{\rho g}\right)$ is called pressure head, $\left(\frac{v^{2}}{2 g}\right)$ is called velocity or kinetic head and $Z$ is called the potential head. |
| Speed of efflux | $v=\sqrt{\frac{2 g h}{1-\frac{A_{2}^{2}}{A_{1}^{2}}}}$ <br> Here, v is the velocity, g is the gravitational acceleration, h is the height, $A_{2}$ is the area of hole and $A_{1}$ is the area of the vessel. |
| Stress | $\sigma=\frac{F}{A}$ <br> here, $\sigma$ is the stress, F is the force and A is the area. |
| Strain | $\varepsilon=\frac{\Delta L}{L}$ <br> here, $\varepsilon$ is the strain, $\Delta L$ is the change in length, and L is the initial length. |
| Young's modulus | $E=\frac{\sigma}{\varepsilon}$ <br> Or $E=\frac{F L}{A \Delta L}$ <br> here, $E$ is the young's modulus, F is the force, L is the initial length, A is the area of cross section and $\Delta L$ is the change in length. |
| Stoke's law | $F=6 \pi \eta r v$ <br> Here, F is the drag experienced by the sphere, r is the radius of the sphere, $\eta$ is the viscosity of the fluid and $v$ is the velocity of the sphere. |
| Terminal velocity | $v=\frac{2}{9}\left(\frac{r^{2}(\rho-\sigma) g}{\eta}\right)$ |


|  | Here, $r$ is the radius of the sphere, $\rho$ is the density of the sphere, $\sigma$ is the density of the fluid, $g$ is the gravitational acceleration and $\eta$ is the viscosity of the fluid. |
| :---: | :---: |
| The formula for magn | Magnetic Effect of Current Formula <br> tic effect of current are as stated below |
| Description | Formula |
| Magnetic field due to a moving point charge | Magnetic field due to a moving point charge is given as $\vec{B}=\frac{\mu_{0} q(\vec{v} \times \vec{r})}{4 \pi r^{3}}$ <br> $\mu_{0}=$ permeability of free space |
| Biot Savart's Law | $d B \propto \frac{I \cdot d l \cdot \sin \theta}{r^{2}}$ |
| Magnetic field due to a straight wire |  <br> The magnetic field due to a straight wire is given as $B=\frac{\mu_{0} I}{4 \pi r}\left(\sin \theta_{1}+\sin \theta_{2}\right)$ |


| Magnetic field due to an infinite straight line | $B=\frac{\mu_{0} I}{2 \pi r}$ |
| :---: | :---: |
| Magnetic field due to a circular loop | $\frac{\mu_{0}\left(N I R^{2}\right)}{2\left(R^{2}+x^{2}\right)^{3 / 2}}$ <br> At centre $B=\frac{\mu_{0} N I}{2 r}$ |
| Magnetic field on the axis of a solenoid | $B=\frac{\mu_{0} N I}{2}\left(\cos \theta_{1}-\cos \theta_{2}\right)$ |
| Ampere's Law | $\oint \vec{B} \cdot \overrightarrow{d l}=\mu_{0} l$ |
| Magnetic field due to a long cylinder | $B=0, r<R$ <br> And $B=\frac{\mu_{0} N I}{2 r}, r \geq R$ |
| Magnetic force acting on a moving point Charge | $\vec{F}=q(\vec{v} \times \vec{B})$ |
| Magnetic force acting on a current-carrying | $\vec{F}=I(\vec{l} \times \vec{B})$ |


| Magnetic Moment of <br> a current carrying <br> loop | $M=N I A$ |
| :--- | :---: |
| The torque acting on <br> a loop | $\vec{\tau}=\vec{M} \times \vec{B}$ |
| Magnetic field due to <br> single pole | $B=\frac{\mu_{0} m}{2 \pi r^{2}}$ |
| Magnetic field on the <br> axis of the magnet | $B=\frac{\mu_{0} 2 M}{4 \pi r^{3}}$ |
| Magnetic field on the <br> equatorial axis of the <br> magnet | $B=\frac{\mu_{0} M}{4 \pi r^{3}}$ |
| Magnetic field at the <br> point $P$ of the <br> magnet | $B=\frac{\mu_{0} M}{4 \pi r^{3}}\left[\sqrt{ }\left(1+\cos ^{2} \theta\right)\right]$ |

## Part 7

## Wave Formula Part 1

Electromagnetic wave equations are given as below

| Description | Formula |
| :--- | :---: |
| Gauss's Law <br> for electricity | $\oint E . d a=\frac{Q}{\epsilon_{0}}$ |
| Gauss's Law <br> for Magnetism | $\oint B . d A=0$ |
| Faraday's Law | $\oint E . d l=-\frac{d \phi}{d t}$ |
| Ampere-Maxw <br> ell Law | $\oint B . d l=\mu_{0} \epsilon_{0} \frac{d \Phi_{E}}{d t}$ |
| Speed of Light <br> in Vacuum | $c=\frac{1}{\sqrt{\mu_{0} \epsilon_{o}}}$ |


| Speed of light in medium | $v=\frac{1}{\sqrt{\mu \epsilon}}$ |
| :---: | :---: |
| Relation <br> between <br> Electric and <br> Magnetic field | $\frac{E_{0}}{B_{0}}=c$ |
| The formula for | Wave Formula 2 <br> wave are as stated below |
| Description | Formula |
| General Equation of Wave Motion | $\frac{\partial^{2} y}{\partial t^{2}}=v^{2} \frac{\partial^{2} y}{\partial x^{2}}$ |
| Wave number | $k=\frac{2 \pi}{\lambda}=\frac{\omega}{v}\left(\mathrm{rad} \mathrm{m}{ }^{-1}\right)$ |
| Phase of a Wave | It is the difference in phases of two particles at any time $t$. $\Delta \phi=\frac{2 \pi}{\lambda} \Delta x$ |
| Speed of <br> Transverse <br> Wave Along a <br> String / Wire | $\begin{gathered} v=\sqrt{\frac{T}{\mu}} \text { where } T=\text { Tension } \\ \mu=\text { mass per unit length } \end{gathered}$ |
| Power <br> Transmitted Along The String By a Sine Wave | Average Power (P) $P=2 \pi^{2} f^{2} A^{2} \mu v$ <br> Intensity $I=\frac{P}{S}=2 \pi^{2} f^{2} A^{2} \rho v$ |
| Longitudinal Displacement of Sound Wave | $\epsilon=A \sin (\omega t-k x)$ |
| Pressure Excess during travelling sound wave | $\begin{gathered} P_{e x}=-B \frac{\partial \epsilon}{\partial x} \\ =(B) \operatorname{Cos}(\omega t-k x) \end{gathered}$ <br> Where $B$ is the Bulk Modulus $P_{e x}$ is the excess pressure |


| Speed of Sound | $C=\sqrt{\frac{E}{\rho}}$ <br> Here, E is elastic modulus $\rho$ is the density of medium |
| :---: | :---: |
| Loudness of Sound | $10\left(\frac{I}{I_{0}}\right) d B$ |
| Intensity at a distance $r$ from a point Source | $I=\frac{P}{4 \pi r^{2}}$ |
| Interference of Sound Wave | $\begin{aligned} & P_{1}=P_{m 1} \operatorname{Sin}\left(\omega t-k x_{1}+\theta_{1}\right) \\ & P_{2}=P_{m 2} \operatorname{Sin}\left(\omega t-k x_{2}+\theta_{2}\right) \end{aligned}$ <br> The Result is the sum of all the pressure. $P_{0}=\sqrt{p_{m_{1}}^{2}+p_{m_{2}}^{2}+2 p_{m_{1}} P_{m 2} \cos \phi}$ |
| For constructive Interference | $\phi=2 \pi n \text { then },=>P_{o}=P_{m_{1}}+P_{m_{2}}$ |
| For destructive interference | $\phi=(2 n+1) \pi$ and $=>P_{o}=\left\|P_{m_{1}}-P_{m_{2}}\right\|$ |
| Close Organ Pipe | $f=\frac{v}{4 l}, \frac{3 v}{4 l}, \frac{5 v}{4 l}, \ldots \frac{(2 n+1) v}{4 l}$ |
| Open organ pipe | $f=\frac{v}{2 l}, \frac{2 v}{2 l}, \ldots \frac{n V}{2 l}$ |
| Beats | Beats Frequency= $f_{1}-f_{2}$ |
| Doppler's Law | The Observed Frequency, $f^{\prime}=f\left(\frac{v-v_{0}}{v-v_{s}}\right)$ <br> Apparent Wavelength, $\lambda^{\prime}=\lambda\left(\frac{v-v_{s}}{v}\right)$ |
| The formula for | Wave Optics Formula <br> wave optics are as stated below |
| Description | Formula |
| The path difference of | $\Delta d=d_{2}-d_{1}$ <br> $\Delta d$ is the path difference |


| two coherent Waves |  |
| :---: | :---: |
| The Path difference of two coherent waves: Interference Maximum | $\Delta d=k . \lambda$ <br> $\Delta d$ is path difference $\lambda$ is the wavelength |
| The path difference of two coherent waves: Interference Minimum | $\Delta d=\frac{(2 \cdot k+1) \cdot \lambda}{2}$ <br> $\Delta d$ is path difference $\lambda$ is the wave length |
| Thin-film interference: Constructive (maximum) | $2 n t \cos r=(n+1 / 2) \lambda$ <br> t is film thickness n is refractive index $r$ is refraction angle $\lambda$ is wave length |
| Thin-Film interference: destructive (minimum) | $2 n t \cos r=n \lambda$. <br> t is film thickness <br> n is refractive index <br> $r$ is refraction angle <br> $\lambda$ is wave length |
| Radii of Newton's Ring | $r=\sqrt{k \cdot R \cdot \lambda} \quad \text { or } \quad r=\frac{\sqrt{((2 . k+1) \cdot R \cdot \lambda)}}{2}$ <br> $r$ is the radius <br> $R$ is the radius of curvature $\lambda$ is the wavelength |
| Light Diffraction | $l=\frac{d^{2}}{4 . \lambda}$ <br> I is the distance from obstacle d is the obstacle size $\lambda$ is wavelength |


| Diffraction grating: maximum (bright stripes) | $d \sin \theta=k \lambda$ <br> d is the lattice constant $\theta$ is the diffraction angle $\lambda$ is the wavelength |
| :---: | :---: |
| Diffraction grating (dark stripes) | $d \sin \theta=(K+1 / 2) \lambda$ <br> $d$ is the lattice constant <br> $\phi$ is the diffraction angle <br> $\lambda$ is the wavelength |
| The formula fo | Work Power and Energy Formula <br> work power energy are as stated below |
| Description | Formula |
| Work done is given by | $W=F \times d$ <br> F is the force d is the displacement |
| Kinetic <br> Energy | $K . E=\frac{1}{2} m v^{2}$ <br> m is the mass of the body. $v$ is the velocity of the body |
| Potential <br> Energy |  |
| Power | $P=\frac{W}{t}$ <br> W is the work done by the body $t$ is the time $P=\frac{\vec{F} \cdot \vec{d} s}{d t}=\vec{F} \cdot \vec{V}$ |
| Conservative Forces | $F=-\frac{d u}{d r}$ |


| Work-Energy theorem | $W_{n e t}=\Delta K$ <br> Where <br> $W_{n e t}$ is the sum of all forces acting on the object $\Delta K$ is the change of kinetic energy |
| :---: | :---: |
| The formula for | Kinetic Theory Formula <br> kinetic theory are as stated below |
| Description | Formula |
| Boltzmann's Constant | $\begin{aligned} & \quad k_{B}=\frac{n R}{N} \\ & k_{B}=\text { Boltzmann's constant } \\ & \mathrm{R}=\text { gas constant } \\ & \mathrm{n}=\text { number of moles } \\ & \mathrm{N}=\text { number of particles in one mole } \end{aligned}$ |
| Total translational Kinetic Energy of Gas | $\begin{aligned} & \quad K \cdot E=\frac{3}{2}(n R T) \\ & R=\text { gas constant } \\ & n=\text { number of moles } \\ & T=\text { absolute temperature } \end{aligned}$ |
| Maxwell distribution law |  $V_{r m s}>V>V_{p}$ <br> $V_{r m s}=\mathrm{RMS}$ speed <br> $V_{p}=$ most probable speed <br> $\mathrm{V}=$ average speed |
| RMS Speed | $\begin{aligned} & \quad V_{r m s}=\sqrt{\frac{3 k t}{m}}=\sqrt{\frac{3 R t}{M}} \\ & \mathrm{R}=\text { universal gas constant } \\ & \mathrm{T}=\text { absolute temperature } \\ & \mathrm{M}=\text { molar mass } \end{aligned}$ |


| Average <br> Speed | $\vec{v}=\sqrt{\frac{8 k t}{\pi m}}=\sqrt{\frac{8 R t}{\pi M}}$ |
| :---: | :---: |
| Most probable speed | $v_{p}=\sqrt{\frac{2 k t}{m}}=\sqrt{\frac{2 R t}{M}}$ |
| Pressure of ideal gas | $p=\frac{1}{3} \rho v^{2}{ }_{r m s}$ |
| Equipartition of energy | For each degree of freedom $K=\frac{1}{2} k_{B} T$ <br> For $f$ degree of freedom $K=\frac{f}{2} k_{B} T$ <br> $k_{B}=$ Boltzmann's constant <br> $\mathrm{T}=$ temperature of gas |
| Internal Energy | For n moles of an ideal gas, internal energy is given as $U=\frac{f}{2}(n R T)$ |
| The formula for | Kinetic Theory of Gases Formula <br> kinetic theory of gases are as stated below |
| Description | Formula |
| Boltzmann's Constant |  |
| Total <br> Translational <br> K.E of Gas | $K . E=\left(\frac{3}{2}\right) n R T$ <br> - n is the number of moles <br> - R is the Universal gas Constant <br> - T is the absolute Temperature |
| Maxwell Distribution Law | $V_{r m s}>V>V p$ <br> - $V_{r m s}$ is the RMS speed <br> - V is the Average Speed. |


|  | - $V p$ is the most probable speed |
| :---: | :---: |
| RMS Speed ( $\left.V_{r m s}\right)$ | $V_{r m s}=\sqrt{\frac{8 k t}{m}}=\sqrt{\frac{3 R T}{M}}$ <br> - $R$ is the universal gas constant. <br> - T is the absolute temperature. <br> - $M$ is the molar mass. |
| Average Speed | $\vec{v}=\sqrt{\frac{8 k t}{\pi m}}=\sqrt{\frac{8 R T}{\pi M}}$ |
| Most <br> Probable <br> Speed $\left(V_{p}\right)$ | $V_{p}=\sqrt{\frac{2 k t}{m}}=\sqrt{\frac{2 R T}{M}}$ |
| The Pressure of Ideal Gas | $P=\frac{1}{3} V_{r m s}^{2}$ <br> - $P$ is the density of molecules |
| Equipartition of Energy | $K=\frac{1}{2} K_{B} T$ for each degree of freedom $\mathrm{K}=\left(\frac{f}{2}\right) K_{B} T$ for molecules having f degrees of freedom <br> - $K_{B}$ is the Boltzmann's Constant <br> - $T$ is the Temperature of the gas |
| Internal Energy | $U=\left(\frac{f}{2}\right) n R T$ <br> - For $n$ moles of an ideal Gas. |

## Part 8



|  | $\begin{gathered} \mathrm{E}=-\mathrm{N}(\mathrm{~d} \phi / \mathrm{dt}) \\ \mathrm{E}=-\mathrm{N}\left(\left(\phi_{1}-\phi_{2}\right) / \mathrm{t}\right) \end{gathered}$ |
| :---: | :---: |
| Induced Current | Induced Current is given as $\mathrm{I}=\mathrm{E} / \mathrm{R}=\mathrm{N} / \mathrm{R}(\mathrm{~d} \phi / \mathrm{dt})=\mathrm{N} / \mathrm{R}\left(\left(\phi_{1}-\phi_{2}\right) / \mathrm{t}\right)$ |
| Self - Induction | Change in the strength of flow of current is opposed by a characteristic of a coil is known as self-inductance. It is given as $\phi=\mathrm{LI}$ Here, $L=$ coefficient of self inductance Magnetic flux rate of change in the coil is given as $d \phi / d t=L d I / d t=-E$ |
| Mutual - Induction | Mutual - Induction is given as $\mathrm{e} 2=\left(\mathrm{d}\left(\mathrm{~N}_{2} \phi_{2}\right) / \mathrm{dt}=\mathrm{M}\left(\mathrm{~d} l_{1}\right) / \mathrm{dt}\right.$ <br> Therefore, $M=\left(\mu_{0} N_{1} N_{2} A\right) / I$ |

## Chemistry Formulas

## Part 1

## Enthalpy Formula

|  | Enthalpy Formula |
| :---: | :---: |
| The formula for enthalpy are as stated below |  |
| Description | Formula |
| Enthalpy | $\begin{aligned} & \mathrm{H}=\mathrm{U}+\mathrm{pV} \\ & \mathrm{U}=\text { Internal energy of system } \\ & \mathrm{p}=\text { Pressure of system } \\ & \mathrm{V}=\text { Volume of system } \end{aligned}$ |
| For change in Enthalpy ( $\Delta \mathrm{H}$ ) | - At isobaric condition: $\begin{aligned} & \text { When } \Delta \mathrm{p}=0 \text {; } \\ & \Delta \mathrm{H}=C_{P}\left(T_{2}-T_{1}\right) \end{aligned}$ <br> - At isochoric condition: $\begin{aligned} & \text { When } \Delta \mathrm{V}=0 \text {; } \\ & \Delta \mathrm{H}=Q_{V}+V \Delta p \end{aligned}$ <br> - At isothermal condition: $\text { When } \Delta \mathrm{T}=0 \text {; }$ $\Delta H=0$ <br> - At Adiabatic condition: $\text { When } Q=0 \text {; }$ $\Delta H=C_{P}\left(T_{2}-T_{1}\right)$ |
| Enthalpy change of a reaction | $\begin{aligned} & \Delta H_{\text {reaction }}=H_{\text {product }}-H_{\text {reactants }} \\ & \Delta H^{\circ}=H_{\text {products }}-H_{\text {reactants }}^{\circ} \\ & =\text { positive } \Delta H-\text { endothermic } \\ & =\text { negative } \Delta H-\text { exothermic } \end{aligned}$ |
| Enthalpy of Reaction from Enthalpies of Formation | The enthalpy of reaction can be given as:- $\Delta H_{r}^{\circ}=\sum v_{B} \Delta H_{f, p r o d u c t s}^{\circ}-\sum v_{B} \Delta H_{f, \text { reactants }}^{\circ}$ <br> $v_{B}$ is the stoichiometric coefficient |
| Estimation of Enthalpy of a reaction from bond Enthalpies | $H=$ Enthalpy required to break reactants into gaseous atoms Enthalpy released to form products from the gasesous atoms |
| Resonance energy | $\begin{aligned} \Delta H_{\text {resonance }}^{\circ} & =\Delta H_{f, \text { experimental }}^{\circ}-\Delta H_{f, \text { calculated }}^{\circ} \\ \Delta H_{\text {resonance }}^{\circ} & =\Delta H_{c, \text { calculated }}^{\circ}-\Delta H_{f, \text { experimental }}^{\circ} \end{aligned}$ |

## Entropy Formula

The formula for entropy are as stated below

| Description | Formula |
| :---: | :---: |
| Entropy | $\Delta S_{\text {system }}=\int_{A}^{B} \frac{d q_{\text {rev }}}{T}$ |
| Entropy calculation for an ideal gas | $\begin{aligned} & \Delta S_{\text {system }}=n c_{v} \ln \frac{T_{2}}{T_{1}}+n R \cdot \ln \frac{V_{2}}{V_{1}} \\ & \text { Also } \\ & \Delta S_{\text {system }}=n c_{P} \ln \frac{T_{2}}{T_{1}}+n R \cdot \ln \frac{V_{2}}{V_{1}} \end{aligned}$ |
| if the reaction of the process is known then we can find $\Delta S_{r x n}$ by using a table of standard entropy values | $\Delta S_{r x n}=\sum \Delta S_{\text {products }}-\sum \Delta S_{\text {reactants }}$ <br> $\Delta S_{r x n}$ - refers to the standard entropy values <br> $\Sigma \Delta$ Sproducts $=$ refers to the sum of the $\Delta$ Sproducts <br> $\Sigma \Delta$ reactants - refers to the sum of the $\Delta$ Sreactants |
| Gibbs free energy | $G_{\text {system }}=H_{\text {system }}-T S_{\text {system }}$ |

## Atomic Mass Formula

The formula for atomic mass are as stated below

| Description | Formula |
| :---: | :---: |
| Atomic Mass | Atomic Mass = Mass of protons + Mass of neutrons + Mass of electrons |
| Mass Number | Mass number = no. of protons + no. of neutrons |
| Relative atomic mass | $R A M=\frac{\text { Mass of one atom of an element }}{\frac{1}{2} \times \text { mass of one carbon atom }}$ |
| Specific gravity | $\text { Specific gravity }=\frac{\text { density of the substance }}{\text { density of water at } 4^{\circ} \mathrm{C}}$ |
| Absolute density | $\begin{aligned} & \text { Absolute density }=\frac{\text { Molar mass of the gas }}{\text { Molar volume of the gas }} \\ & \rho=\frac{P M}{R T} \end{aligned}$ |
| Vapor density | V. D. $=\frac{d_{\text {gas }}}{d_{H_{2}}}=\frac{P M_{\frac{g a s}{k r}}}{P M_{\frac{H_{2}}{d \tau}}}=\frac{M_{\text {gas }}}{M_{H_{2}}}=\frac{M_{\text {gas }}}{2}$ |


|  | $\therefore M_{\text {gas }}=2 \mathrm{~V} . D$. |
| :---: | :---: |
| Molarity | $M=\frac{w \times 1000}{(\text { Mol. wt of solute }) \times V_{\text {in } m l}}$ |
| Molality | $m=\frac{\text { number of moles of solute }}{\text { mass of solvent in gram }} \times 1000=\frac{1000 \times w_{1}}{M_{1} \times w_{2}}$ |
| Mole fraction | - Mole fraction of solution $\left(x_{1}\right)=\frac{n}{n+N}$ <br> - Mole fraction of solvent $\left(x_{2}\right)=\frac{N}{n+N}$ $x_{1}+x_{2}=1$ |
| \% Calculation: | - $\% w / w=\frac{\text { mass of solute in } \mathrm{gm}}{\text { mass of solution in } g m} \times 100$ <br> - $\% w / v=\frac{\text { mass of solute in } g m}{\text { Volume of solution in } m l} \times 100$ <br> - $\% v / v=\frac{\text { Volume of solute in } m l}{\text { Volume of solution }} \times 100$ |
| Derived conversion | - Mole fraction of solute into molarity of solution $M=\frac{x_{2} \rho \times 1000}{x_{1} M_{1}+M_{2} x_{2}}$ <br> - Molarity into mole fraction $x_{2}=\frac{M M_{1} \times 1000}{\rho \times 1000-M M_{2}}$ <br> - Mole fraction into molality $m=\frac{x_{2} \times 1000}{x_{1} M_{1}}$ <br> - Molality into mole fraction $x_{2}=\frac{m M_{1}}{1000+m M_{1}}$ <br> - Molality into molarity $M=\frac{m \rho \times 1000}{1000+m M_{2}}$ <br> - Molarity into molality $m=\frac{M \times 1000}{1000 \rho-M M_{2}}$ <br> Here $M_{1}$ and $M_{2}$ are molar masses of solvent and solute <br> $\rho$ is density of solution <br> $M$ is molarity <br> $m$ is molality <br> $x_{1}$ is mole fraction of solvent <br> $x_{2}$ is mole fraction of solute |
| Average atomic mass | $A_{x}=\frac{a_{1} x_{1}+a_{2} x_{2}+\ldots \ldots+a_{n} x_{n}}{100}$ |
| Mean molar mass | $M_{\text {avg }}=\frac{M_{1} n_{1}+M_{2} n_{2}+\ldots M_{n} n_{n}}{n_{1}+n_{2}+\ldots . . n_{n}}$ |


| Normality | - $N=\frac{\text { Number of equivalents of solute }}{\text { Volume of solution }}$ <br> - $N=$ Molarity $\times v . f$ |
| :---: | :---: |
| At equivalence point | - $N_{1} V_{1}=N_{2} V_{2}$ <br> - $n_{1} M_{1} V_{1}=n_{2} M_{2} V_{2}$ |
| Oxidation Number | Oxidation Number $=$ number of electrons in the valence shell number of electrons lef taf ter bonding |
| Equivalent weight | $E=\frac{\text { Atomic weight }}{\text { Valency factor }}$ |
| Concept of number of equivalents | - No. of equivalents of solute $=\frac{W t}{E q . w t .}=\frac{W}{E}=\frac{W}{M / n}$ <br> - No. of equivalents of solute $=$ No. of moles of solute $\times$ v.f. |
| Measurement of Hardness | - Hardness $=\frac{\text { mass of } \mathrm{CaCO}_{3}}{\text { Total mass of water }} \times 10^{6}$ |
| The formula for atomi | Atomic Structure Formula tructure are as stated below |
| Description | Formula |
| Planck's Quantum Theory | Energy of one photon $=h v=\frac{h c}{\lambda}$ |
| Photoelectric effect: | $h v=h v_{0}+\frac{1}{2} m_{e} v^{2}$ |
| Bohr's Model for Hydrogen like atoms | - $m v r=n=\frac{h}{2 \pi}$ <br> - $E_{n}=-\frac{E_{1}}{n^{2}} z^{2}=-2.178 \times 10^{-18} \frac{z^{2}}{n^{2}} \mathrm{~J} /$ atom $=-13.6 \frac{z^{2}}{n^{2}} \mathrm{eV}$ <br> - $E_{1}=\frac{-2 \pi^{2} m e^{4}}{n^{2}}$ <br> - $r_{n}=\frac{n^{2}}{Z} \times \frac{h^{2}}{4 \pi^{2} e^{2} m}=\frac{0.529 \times n^{2}}{Z} A^{0}$ <br> - $v=\frac{2 \pi z e^{2}}{n h}=\frac{2.18 \times 10^{6} \times z}{n} \mathrm{~m} / \mathrm{s}$ |
| De-Broglie wavelength | $\lambda=\frac{h}{m c}=\frac{h}{p}$ (For photon) |
| Wavelength of emitted photon | $\frac{1}{\lambda}=R Z^{2}\left(\frac{1}{n_{1}^{2}}-\frac{1}{n_{2}^{2}}\right)$ |


| Number of photons emitted by a sample of H atom | $E=n h v$ <br> Where n is the number of photons emitted $h$ is the Planck's constant $v$ is the frequency |
| :---: | :---: |
| Heisenberg's uncertainty principle | - $\Delta x . \Delta p>\frac{h}{4 \pi}$ <br> - $m \Delta x \cdot \Delta v \geq \frac{h}{4 \pi}$ <br> - $\Delta x . \Delta v \geq \frac{h}{4 \pi m}$ |
| Quantum Number | - Principle quantum number - $(n=1,2,3,4,5 \ldots \infty)$ <br> - Orbital angular momentum of electron in any orbit $=\frac{n h}{2 \pi}$ <br> - Azimuthal quantum number $(l)=0,1,2,3, \ldots(n-1)$ <br> - Magnetic quantum number (m)=-I,.....-1,0,1.....+। <br> - Spin quantum number ( s ) $=+1 / 2,-1 / 2$ <br> - Number of orbitals in subshell $=2 l+1$ <br> - Maximum number of electrons in particular subshell $=2(2 l+1)$ <br> - Orbital angular momentum $L=\frac{h}{2 \pi} \sqrt{l(l+1)}=\hbar \sqrt{l(l+1)}$ <br> - $\hbar=\frac{h}{2 \pi}$ |
| The formula for molar | Molar Mass Formula |
| Description | Formula |
| Molar mass | $\mathrm{M}=\frac{m}{n}$ <br> M is the molar mass, $m$ is the mass of a substance (in grams), n is the number of moles of a substance. |
| Molar mass of an element | Molar mass $=$ Molar mass constant $\times$ Relative atomic mass |
| molar mass from colligative properties data | $\mathrm{M}=\frac{\Delta T_{f}}{K_{f}}$ |
| When elevation of boiling point is given | $\begin{array}{\|l} \Delta T b=K b m \\ \mathrm{~m}=1000 \times \mathrm{w} 2 / \mathrm{w} 1 \times \mathrm{M} 2 \\ \Delta T b=K b \times 1000 \times \mathrm{w} 2 / \mathrm{w} 1 \times \mathrm{M} 2 \end{array}$ |
| When depression of freezing point is given | $\begin{aligned} & \Delta T f=K f m \\ & \Delta T f=K f \times 1000 \times \mathrm{w} 2 / \mathrm{w} 1 \times \mathrm{M} 2 \end{aligned}$ |


| Molarity | $M=\frac{w \times 1000}{(\text { Mol. wt of solute }) \times V_{\text {in } m l}}$ |
| :---: | :---: |
| Molality | $m=\frac{\text { number of moles of solute }}{\text { mass of solvent in gram }} \times 1000=\frac{1000 \times w_{1}}{M_{1} \times w_{2}}$ |
| Average atomic mass | $A_{x}=\frac{a_{1} x_{1}+a_{2} x_{2}+\ldots \ldots+a_{n} x_{n}}{100}$ |
| Mean molar mass | $M_{\text {avg }}=\frac{M_{1} n_{1}+M_{2} n_{2}+\ldots M_{n} n_{n}}{n_{1}+n_{2}+\ldots n_{n}}$ |
| The formula for stoich | Stoichiometry Formula <br> metry are as stated below |
| Description | Formulas |
| Relative atomic mass | $\text { Relative atomic mass }(\text { R. A. } M)=\frac{\text { Mass of one atom of an element }}{\frac{1}{12} \times \text { mass of one Carbon atom }}=\text { Total number os }$ |
| Density | $\text { Specific gravity }=\frac{\text { density of the substance }}{\text { density of water at } 4^{\circ} \mathrm{C}}$ |
| For Gases: | $\begin{gathered} \text { Absolute density }\left(\frac{\text { mass }}{\text { volume }}\right)=\frac{\text { Molar mass of the gas }}{\text { Molar Volume of the gas }} \\ =>\rho=\frac{P M}{R T} \\ \text { Vapor density } V . D . .=\frac{d_{\text {gas }}}{d_{H_{2}}}=\frac{P M_{\text {gas }}}{P M_{\frac{H_{2}}{R I}}^{R I}}=\frac{M_{\text {gas }}}{M_{H_{2}}} \\ M_{\text {gas }}=2 \mathrm{~V} \cdot D \end{gathered}$ |
| Molarity (M): | $\operatorname{Molarity}(M)=\frac{w \times 1000}{(\text { Mol. wt of Solute }) \times V_{\text {in } m t}}$ |
| Moality (m): | $\text { Molality }=\frac{\text { number of moles of solute }}{\text { mass of solvent in gram }} \times 1000=1000 \frac{W_{1}}{M_{1} W_{2}}$ |
| \% Calculation | $\begin{gathered} \% \frac{w}{w}=\frac{\text { mass of solute in } \mathrm{gm}}{\text { mass of solution in } \mathrm{gm}} \times 100 \\ \% \frac{w}{v}=\frac{\text { Mass of solute in } \mathrm{gm}}{\text { Volume of solution in } m l} \times 100 \\ \% \frac{v}{v}=\frac{\text { Volume of solute in } \mathrm{ml}}{\text { Volume of solution }} \times 100 \end{gathered}$ |
| Average/ Mean atomic mass: | $A_{x}=\frac{a_{1} x_{1}+a_{2} x_{2}+\ldots+a_{n} X_{n}}{100}$ |
| Mean molar mass or molecular Mass | $M_{\text {avg }}=\frac{n_{1} M_{1}+n_{2} M_{2}+\ldots . n_{n} M_{n}}{n_{1}+n_{2}+n_{3}+\ldots n_{n}}$ |
| Normality ( N ) | $\operatorname{Normality}(N)=\frac{\text { Number of equivalents of solute }}{\text { Volume of Sodium (in liters) }}$ |


| Measurement of Hardness | $\text { Hardness in ppm }=\frac{\text { mass of } \mathrm{CaCO}_{3}}{\text { Total Mass of water }} \times 10^{6}$ |
| :---: | :---: |
| Molarity in mole Fraction | $x_{2}=\frac{M M_{1} \times 1000}{\rho \times 1000-M M_{2}}$ |
| Mole Fraction into molality | $m=\left(\frac{x_{2} \times 1000}{x_{1} M_{1}}\right)$ |
| Molality into mole fraction | $x_{2}=\frac{m M_{1}}{1000+m M_{1}}$ |
| Molality into molarity | $M=\frac{m_{\rho} \times 1000}{1000+m M_{2}}$ |
| Relation between molarity and molality | $m=\frac{M \times 1000}{1000 \rho-M M_{1}}$ <br> Where $\rho$ is the density of solution in ( $\mathrm{gm} / \mathrm{mL}$ ). $M_{1}$ is molecular weight of solute $m$ is the molality and $M$ is the molarity |
| Y-Map |  |

## Part 2

## Thermodynamics Formulas

The formula for thermodynamics are as stated below

| Description | Formula |
| :--- | ---: |
| Various processes in | Isothermal process: $\mathrm{T}=$ constant |
| Thermodynamic | $\mathrm{dT}=0$ |
|  | $\Delta \mathrm{~T}=0$ |
|  |  |
|  | Isochoric process: $\mathrm{V}=\mathrm{constant}$ |
| $\mathrm{dV}=0$ |  |
| $\Delta \mathrm{~V}=0$ |  |
|  |  |
|  | Isobaric process: $\mathrm{P}=\mathrm{constant}$ |
| $\mathrm{dP}=0$ |  |
|  |  |


|  | $\Delta P=0$ <br> Adiabatic process: $\mathrm{q}=0$ <br> or the heat exchange with surrounding is zero |
| :---: | :---: |
| Sign convention | When work is done on the system: Positive When work is done by the system: Negative |
| Laws of Thermodynamics | - $1^{\text {st }}$ law of Thermodynamics $\Delta U=\left(U_{2}-U_{1}\right)=q+w$ <br> - $2^{\text {nd }}$ law of Thermodynamics $\Delta S_{\text {universe }}=\Delta S_{\text {system }}+\Delta S_{\text {surrounding }}>0$ <br> This equation is for spontaneous processes. <br> - $3^{\text {rd }}$ law of Thermodynamics $\mathrm{S}-\mathrm{S}_{0}=k_{\mathrm{B}} \ln \Omega$ <br> $S$ is the entropy of the system. $S_{0}$ is the initial entropy. $k_{B}$ denotes the Boltzmann constant. <br> $\Omega$ refers to the total number of microstates that are consistent with the system's macroscopic configuration. |
| Law of Equipartition Energy | $\begin{aligned} & U=\frac{f}{2} n R T \\ & \Delta E=\frac{f}{2} n R(\Delta T) \end{aligned}$ <br> Where, $f$ is degrees of freedom for that gas. |
| Total heat capacity | $C_{T}=\frac{\Delta q}{\Delta T}=\frac{d q}{d T}$ |
| Molar heat capacity | $\begin{aligned} & C=\frac{\Delta q}{n \Delta T}=\frac{d q}{n d T} \\ & C_{p}=\frac{\gamma R}{\gamma-1} \quad C_{v}=\frac{R}{\gamma-1} \\ & \hline \end{aligned}$ |
| Specific heat capacity | $S=\frac{\Delta q}{m \Delta T}=\frac{d q}{m d T}$ |
| Application of $1^{\text {st }}$ Law of Thermodynamics | $\begin{aligned} & \Delta U=\Delta Q+\Delta W \\ & \Rightarrow \Delta W=-P \Delta V \quad(\therefore \Delta U=\Delta Q-P \Delta V) \end{aligned}$ |
| Isothermal Reversible expansion/compressio n of an ideal gas | $W=-n R T \ln \left(\frac{V_{f}}{V_{i}}\right)$ |
| Reversible/irreversible isochoric processes | $\begin{array}{\|l\|} \hline \text { Since } d V=0 \\ \text { So, } d W=-P_{\text {ext }} \cdot d V=0 \\ \hline \end{array}$ |
| Reversible isobaric process | $W=P\left(V_{f}-V_{i}\right)$ |
| Adiabatic reversible expansion | $T_{2} V_{2}^{\gamma-1}=T_{1} V_{1}^{\gamma-1}$ |
| Reversible work | $W=\frac{P_{2} V_{2}-P_{1} V_{1}}{\gamma-1}=\frac{n R\left(T_{2}-T_{1}\right)}{\gamma-1}$ |
| Irreversible Work | $W=\frac{P_{2} V_{2}-P_{1} V_{1}}{\gamma-1}=\frac{n R\left(T_{2}-T_{1}\right)}{\gamma-1}=n C_{v}\left(T_{2}-T_{1}\right)=-P_{e x t}\left(V_{2}-V_{1}\right)$ |



|  | $\frac{r_{1}}{r_{2}}=\frac{\sqrt{d_{2}}}{\sqrt{d_{1}}}=\frac{\sqrt{M_{2}}}{\sqrt{M_{1}}}=\sqrt{\frac{V \cdot D_{2}}{V_{V}}}$ <br> Van der wall's Equation |
| :--- | :---: |



|  | $K_{a}=\frac{\left[H^{+}\right]\left[A^{-}\right]}{H A}=\frac{[C \alpha][C \alpha]}{C(1-\alpha)}=\frac{C \alpha^{2}}{1-\alpha}$ <br> - If $\alpha \ll 1$, then $1-\alpha \cong 1$ or $K_{a}=c \alpha^{2}$ $\alpha=\sqrt{\frac{K_{a}}{C}}=\sqrt{K_{a} \times V}$ <br> - Similarly for a weak base, $\alpha=\sqrt{\frac{K_{b}}{c}}$ <br> Higher the value of $K_{a} / K_{b}$, stronger is the acid/base |
| :---: | :---: |
| Acidity and pH scale | - $\mathrm{pH}=-\log a_{H^{+}}$ <br> Here $a_{H^{+}}$is the activity of $H^{+}$ions = molar concentration for dilute solution <br> - $p H=-\log \left[H^{+}\right] \quad\left[H^{+}\right]=10^{-p H}$ <br> - $\mathrm{pOH}=-\log \left[\mathrm{OH}^{-}\right][\mathrm{OH}-]=10^{-\mathrm{pOH}}$ <br> - $p K a=-\log K a \quad K a=10^{p K a}$ <br> - $p K b=-\log K b \quad K b=10^{-p K b}$ |
| pH Calculations of Different Types of Solutions: | - Strong acid solution: <br> If concentration is greater than $10^{-6} \mathrm{M}$ <br> In this case $H^{+}$ions coming from water can be neglected, If concentration is less than $10^{-6} \mathrm{M}$ <br> In this case $H^{+}$ions coming from water cannot be neglected <br> - Strong base solution: <br> Using similar method as in part (a) calculate first $\left[\mathrm{OH}^{-}\right.$] and then use $\left[\mathrm{H}^{+}\right] \times\left[\mathrm{OH}^{-}\right]=10^{-14}$ |
| pH of mixture of two strong acids: | - Number of $\mathrm{H}+$ ions from I-solution $=N_{1} V_{1}$ <br> - Number of $\mathrm{H}+$ ions from II-solution $=N_{2} V_{2}$ $\left[H^{+}\right]=N=\frac{N_{1} V_{1}+N_{2} V_{2}}{V_{1}+V_{2}}$ |
| pH of mixture of two strong bases: | $\left[O H^{-}\right]=N=\frac{N_{1} V_{1}+N_{2} V_{2}}{V_{1}+V_{2}}$ |
| pH of mixture of a strong acid and a strong base: | - if $N_{1} V_{1}>N_{2} V_{2}$, then the solution will be acidic in nature. So, $\left[H^{+}\right]=N=\frac{N_{1} V_{1}-N_{2} V_{2}}{V_{1}+V_{2}}$ |


|  | - If $N_{2} V_{2}>N_{1} V_{1}$, then the solution will be basic in nature. So, $\left[O H^{-}\right]=N=\frac{N_{2} V_{2}-N_{1} V_{1}}{V_{1}+V_{2}}$ |
| :---: | :---: |
| pH of a weak acid(monoprotic) solution: | $K_{a}=\frac{\left[H^{+}\right][O H]^{-}}{[H A]}=\frac{\mathrm{Ca}^{2}}{1-\alpha}$ <br> If $\alpha \ll 1 \Rightarrow(1-\alpha) \approx 1$ $\begin{gathered} K_{a} \approx C \alpha^{2} \\ \alpha=\sqrt{\frac{K_{a}}{C}} \end{gathered}$ <br> Here $\alpha<0.1$ or $10 \%$ |
| Relative Strength of two acids: | $\frac{\left[H^{+}\right] \text {furnished by I acid }}{\left[H^{+}\right] \text {furnished by II acid }}=\frac{c_{1} \alpha_{1}}{c_{2} \alpha_{2}}=\sqrt{\frac{k_{a_{1}} c_{1}}{k_{a_{2}} c_{2}}}$ |
| Hydrolysis of polyvalent anions or cations | $\begin{aligned} & \text { For }\left[\mathrm{Na}_{3} \mathrm{PO}_{4}\right]=C \\ & K_{a 1} \times K_{h 3}=K_{w} \\ & K_{a 2} \times K_{h 2}=K_{w} \\ & K_{a 3} \times K_{h 1}=K_{w} \end{aligned}$ <br> Generally, pH is calculated only using the first step hydrolysis $\begin{gathered} K_{h 1}=\frac{C h^{2}}{1-h} \approx C h^{2} \\ h=\sqrt{\frac{K_{h 1}}{c}} \Rightarrow\left[O H^{-}\right]=c h=\sqrt{K_{h 1} \times c} \Rightarrow\left[H^{+}\right]=\sqrt{\frac{K_{w} \times K_{a 3}}{C}} \\ \therefore p H=\frac{1}{2}\left[p K_{w}+p K_{a 3}+\log \log C\right] \end{gathered}$ |
| Buffer Solution: | - Acidic Buffer: e.g., $\mathrm{CH}_{3} \mathrm{COOH}$ and $\mathrm{CH}_{3} \mathrm{COONa}$ (weak acid and salt of its conjugate base) $p H-p K_{a}+\log \log \frac{[\text { salt }]}{[\text { Acid }]}$ <br> - Basic Buffer: e.g., $\mathrm{NH}_{4} \mathrm{OH}+\mathrm{NH}_{4} \mathrm{Cl}$ (weak base and salt of its conjugate acid) $p O H=p K_{b}+\log \log \frac{[\text { Salt }]}{[\text { Base }]}$ |
| Solubility Product: | $K_{s p}=(x s)^{x}(y s)^{y}=x^{x} \cdot y^{y} \cdot(s)^{x+y}$ |
|  | Charles's Law |
| The formula for Charle's law are as stated below |  |


| Description | Formulas |
| :---: | :---: |
| Charles' law is expressed as | $V \alpha T \text { or } \frac{V_{1}}{T_{1}}=\frac{V_{2}}{T_{2}},$ <br> Where $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ are initial and final volume and $T_{1}$ and $T_{2}$ are initial and final temperatures. |
| Derivation of Charles' law | $\begin{gather*} V \alpha T \\ \frac{V}{T}=\text { constant }=k \\ \frac{V_{1}}{T_{1}}=k-----(I) \text { and } \frac{V_{2}}{T_{2}}=k \tag{II} \end{gather*}$ <br> Where $V_{1}$ and $T_{1}$ are initial volume and temperature and $V_{2}$ and $T_{2}$ are the final volume and temperature. <br> Equating equations (I) and (II), $\frac{V_{1}}{T_{1}}=\frac{V_{2}}{T_{2}}=k$ <br> Hence, we can generalize the formula and write it as: $\frac{\left(V_{1}\right)}{\left(T_{1}\right)}=\frac{\left(V_{2}\right)}{\left(T_{2}\right)}$ |
| Gay-Lussac's Law | At constant volume, $\begin{gathered} P \propto T \\ \frac{P_{1}}{T_{1}}=\frac{P_{2}}{T_{2}} \end{gathered}$ |
| Ideal gas Equation | $\begin{gathered} P V=n R T \\ P V=\frac{w}{m} R T \text { Or } P m=d R T \end{gathered}$ |
| Boyle's Law | At Constant Temperature $\begin{gathered} V \propto \frac{1}{P} \\ P_{1} V_{1}=P_{2} V_{2} \\ \hline \end{gathered}$ |
| Amagat's Law of partial volume | $V=V_{1}+V_{2}+V_{3}+\ldots V n$ |

## Part 3

## Electrochemistry Formula

The formula for electrochemistry are as stated below

| Description | Formula |
| :---: | :---: |
| Gibbs Free energy change | - $\Delta G=-n F E_{\text {cell }}$ <br> - $\Delta G^{0}=-n F E_{\text {cell }}^{0}$ |
| Nernst Equation | Effect of concentration and temp on emf of cell <br> where $Q$ is reaction quotient $\begin{aligned} & \Delta G=\Delta G^{0}+R T \ln Q \\ & \Delta G^{0}=-R T \ln K_{e q} \\ & E_{\text {cell }}=E_{\text {cell }}^{0}-\frac{R T}{n F} \ln Q \\ & E_{\text {cell }}=E_{\text {cell }}^{0}-\frac{2.303 R T}{n F} \log Q \\ & E_{\text {cell }}=E_{\text {cell }}^{0}-\frac{0.0591}{n} \log Q \end{aligned}$ <br> - At chemical equilibrium $\begin{gathered} \Delta G=0 ; \quad E_{\text {cell }}=0 \\ \log K_{e q}=\frac{n E_{\text {cell }}^{0}}{0.0591} \\ E_{\text {cell }}^{0}=\frac{0.0591}{n} \log K_{e q} \end{gathered}$ <br> - For an electrode: $E_{M^{n+} / M}=E_{M^{n+} / M}^{0}-\frac{2.303 R T}{n F} \log 1 /\left[M^{n+}\right]$ |
| Concentration Cell | $E_{\text {cell }}^{\circ}=0$ <br> - Electrolyte Concentration cell $\begin{array}{r} \text { (eg., } \left.Z n(s) / Z n^{2+}\left(c_{1}\right) \\| Z n^{2+}\left(c_{2}\right) / Z n(s)\right): \\ E=\frac{0.0591}{2} \log \frac{c_{2}}{c_{1}} \end{array}$ <br> - Electrode Concentration Cell $\begin{gathered} \text { (e.g., Pt, } \left.H_{2}\left(P_{1} \mathrm{~atm}\right) / H^{+}(1 \mathrm{M}) / H_{2}\left(P_{2} \mathrm{~atm}\right) / P t\right) \text { : } \\ E=\frac{0.0591}{2} \log \frac{P_{1}}{P_{2}} \end{gathered}$ |


|  |  |
| :---: | :---: |
| Faraday's law of electrolysis: | - First law: <br> The amount of chemical reaction (w) is proportional to the quantity of electricity passed (q) through the electrolyte. $\begin{aligned} & w \propto q \\ & w=z q \\ & w=Z \end{aligned}$ <br> Here $Z$ is Electrochemical equivalent of substance <br> - Second law: $\begin{aligned} & \quad W \propto E \\ & \frac{W}{E}=\text { constant } \\ & \frac{W_{1}}{E_{1}}=\frac{W_{2}}{E_{2}}=\ldots=\frac{W_{n}}{E_{n}} \\ & \frac{W}{E}=\frac{i \times t \times \text { currentefficiency factor }}{96500} \\ & \text { current efficiency }=\frac{\text { actual mass deposited }}{\text { Theoretical mass deposited }} \times 100 \end{aligned}$ |
| Conductance: | - Conductance $=\frac{1}{\text { Resistance }}$ <br> - Specific conductance or conductivity: $K=\frac{1}{\rho}$ <br> Here, $K$ is specific conductance <br> - Equivalent conductance: $\lambda_{E}=\frac{K \times 1000}{\text { Normality }}$ <br> - Molar conductance: $\lambda_{m}=\frac{K \times 1000}{\text { Molarity }}$ <br> - Specific conductance $=$ conductance $\times \frac{l}{a}$ |
| Application of Kohlrausch law | - Calculation of $\lambda_{M}^{0}$ of weak electrolytes: $\lambda_{M\left(\mathrm{CH}_{3} \mathrm{COOH}\right)}^{0}=\lambda_{M\left(\mathrm{CH}_{3} \mathrm{COONa}\right)}^{0}+\lambda_{M(\mathrm{HCl})}^{0}-\lambda_{M(\mathrm{NaCl})}^{0}$ <br> - To calculate degree of dissociation of a weak electrolyte $\alpha=\frac{\lambda_{m}^{c}}{\lambda_{m}^{0}} ; \quad K_{e q}=\frac{c \alpha^{2}}{1-\alpha}$ |


|  | - Solubility of sparingly soluble salt \& their $K_{s p}$ $\begin{gathered} \lambda_{M}^{c}=\lambda_{M}^{\infty}=k \times \frac{1000}{\text { solubility }} \\ K_{s p}=S^{2} \end{gathered}$ <br> - Transport Number: $t_{c}=\left[\frac{\mu_{c}}{\mu_{c}+\mu_{a}}\right], \quad t_{a}=\left[\frac{\mu_{a}}{\mu_{a}+\mu_{c}}\right]$ <br> - Here $t_{c}$ is Transport Number of cation and $t_{a}$ is the transport number of anion. |
| :---: | :---: |
| The formula for idea | Ideal Gas Equation Formula gas are as stated below |
| Description | Formula |
| Ideal gas law is expressed as: | $P V=n R T$ <br> where, <br> $P$ is the pressure <br> $V$ is the volume <br> n is the amount of substance <br> $R$ is the ideal gas constant. |
| Derivation of Ideal gas law | Ideal gas law combines three laws: <br> - Boyle's Law: Vœ1/P <br> - Charles' Law: $V \propto T$ <br> - Avogadro's Law: $V \propto n$ <br> Combining these above three Equation we get $V \propto \frac{n T}{P}$ <br> The above equation shows that volume is proportional to the number moles and the temperature while inversely proportional to the pressure. <br> This expression can be rewritten as follows: $V=\frac{R n T}{P}$ <br> Multiplying both sides of the equation by P to Clear off the fraction, We get $P V=n R T$ <br> The Above equation is known as the ideal Gas Equation. |
| Molar From of $P V=n R T$ | $n=\frac{m}{M}$, $\mathrm{m}=$ total mass of the gas, $\mathrm{M}=$ Molar mass |


|  | $\begin{aligned} \text { Density } \rho & =\frac{m}{V}, \\ p V & =\frac{m}{M} R T, \\ p=\frac{m R T}{V M}, p & =\rho \frac{R}{M} T \end{aligned}$ |
| :---: | :---: |
| Combined Gas law can be Stated as | $\frac{P_{1} V_{1}}{T_{1}}=\frac{P_{2} V_{2}}{T_{2}}$ |
| If we want to use $N$ number of molecules instead of $n$ moles, we can write the ideal gas law as | $P V=N k_{b} T$ |
| The energy possessed by the gas is in the kinetic energy of the molecules of the gas | $E=\frac{3}{2} n R T$ |
| Avogadro's Constant | Avogadro's Constant $\left(N_{A}\right)$ is the ratio of the total number of molecules $(N)$ to the total moles $(n)$. $N_{A}=\frac{N}{n}=\frac{N}{\frac{P V}{R T}}$ |
| The formula for diffusid | Diffusion Formula <br> on are as stated below |
| Description | Formula |
| Diffusion Formula | $Q_{s}=-D_{s} d s / d x$ <br> Where $Q_{s}$ is the rate of movement of matter, momentum or energy through a unit normal area. <br> $-D_{s}$ is the diffusion coefficient. <br> $d s / d x$ is the gradient of mass, momentum or energy in the medium. |
| Graham's Law | Rate of diffusion $r \propto \frac{1}{\sqrt{d}}$ <br> D= Density of Gas $\frac{r_{1}}{r_{2}}=\frac{\sqrt{d_{2}}}{\sqrt{d_{1}}}=\frac{\sqrt{M_{2}}}{\sqrt{M_{1}}}=\sqrt{\frac{V \cdot D_{2}}{V \cdot D_{1}}}$ |


| Van der Waals Equation | $\left(P+\frac{a n^{2}}{V^{2}}\right)(V-n b)=n R T$ |
| :---: | :---: |
| Critical Constant | $V_{c}=3 b, P_{c}=\frac{a}{27 b^{2}}, T_{c}=\frac{8 a}{27 R b}$ |
| Graham's Law for comparison between two Gases | $\frac{r_{\text {Gas }} A}{r_{G a s} B}=\frac{\left(M_{\text {Gas }}\right)^{\frac{1}{2}}}{\left(M_{\text {Gas } A}\right)^{\frac{1}{2}}}$ |
| The formula for De-B | De-Broglie's Formula <br> roglie are as stated below |
| Description | Formula |
| The de-Broglie's Equation | $\lambda=h / m v,$ <br> Where $\lambda$ is wavelength, $h$ is Planck's constant, $m$ is the mass of a particle, moving at a velocity v . |
| Derivation of De-Broglie's equation | - Plank's quantum theory relates the energy of an electromagnetic wave to its wavelength or frequency. $E=h v=\frac{h c}{\lambda} \ldots \ldots . .(1)$ <br> Einstein related the energy of particle matter to its mass and Velocity, as $E=m c^{2} \ldots \ldots \ldots . . \text { (2) }$ <br> As the Smaller particle exhibits dual nature, and energy being the same, de Broglie Equation as $E=\frac{h c}{\lambda}=m v^{2} \quad \text { then, } \frac{h}{\lambda}=m v$ <br> This is the momentum of a particle with its wavelength and this equation is known as De-Broglie's Equation. |
| De-Broglie's Wavelength | $\lambda=\frac{h}{m v}=\frac{h}{\text { momentum }}=\frac{h}{p}$ |
| Relation between de Broglie Equation and Bohr's Hypothesis of Atom: | $m v=\frac{n h}{2 \Pi r} \quad$ or $\quad m v r=n \times\left(\frac{h}{2 \Pi}\right)$ |
| Thermal De-Broglie Wavelength | The thermal de Broglie wavelength ( $\lambda$ th) is approximately the average de Broglie wavelength of the gas particles in an ideal gas at the specified temperature. |


|  | $\lambda_{t h}=\frac{h}{\sqrt{2 \pi m k_{b} T}}$ $\lambda_{t h}=\frac{h}{\sqrt{2 \pi m k_{b} T}}$ where, $\mathrm{h}=$ Planck constant, $\mathrm{m}=$ mass of a gas particle, $k_{b}=$ Boltzmann constant, $\mathrm{T}=$ temperature of the gas, <br> where, <br> h = Planck constant, <br> $\mathrm{m}=$ mass of a gas particle, <br> $k_{b}=$ Boltzmann constant, <br> $\mathrm{T}=$ temperature of the gas, |
| :---: | :---: |
| De Broglie's in terms of kinetic energy | $\lambda=\frac{h}{\sqrt{2 m K}}$ |

