

CHAPTER 07 TRIANGLES

SUBJECT: MATHEMATICS

MAX. MARKS : 40

CLASS : IX

DURATION : 1½ hrs

General Instructions:

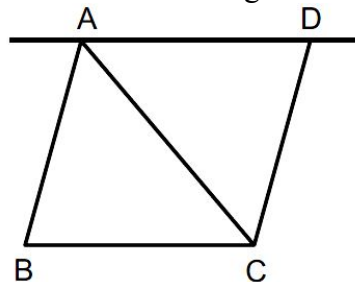
- (i). All questions are compulsory.
- (ii). This question paper contains 20 questions divided into five Sections A, B, C, D and E.
- (iii). **Section A** comprises of 10 MCQs of 1 mark each. **Section B** comprises of 4 questions of 2 marks each. **Section C** comprises of 3 questions of 3 marks each. **Section D** comprises of 1 question of 5 marks each and **Section E** comprises of 2 Case Study Based Questions of 4 marks each.
- (iv). There is no overall choice.
- (v). Use of Calculators is not permitted

SECTION – A

Questions 1 to 10 carry 1 mark each.

1. If $\triangle ACB \cong \triangle EDF$, then which of the following equations is/are true?
 (I) $AC = ED$
 (II) $\angle C = \angle F$
 (III) $AB = EF$
 (a) Only (I) (b) (I) and (III) (c) (II) and (III) (d) All of these

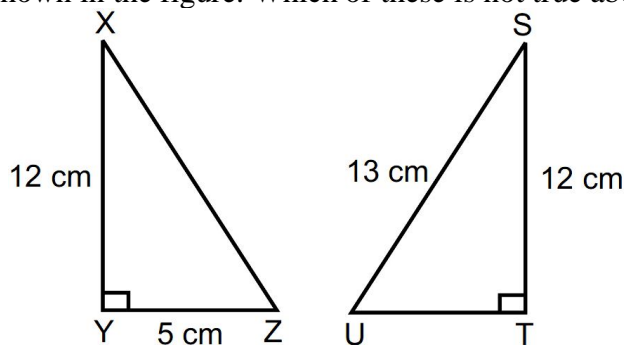
2. In a triangle (as shown in fig). $AB = CD$, $AD = BC$ and AC is the angle bisector of $\angle A$, then which among the following conditions is true for congruence of $\triangle ABC$ and $\triangle CDA$ by SAS rule?



- (a) $\angle A = \angle D$ (b) $\angle B = \angle A$ (c) $\angle B = \angle D$ (d) $\angle C = \angle A$

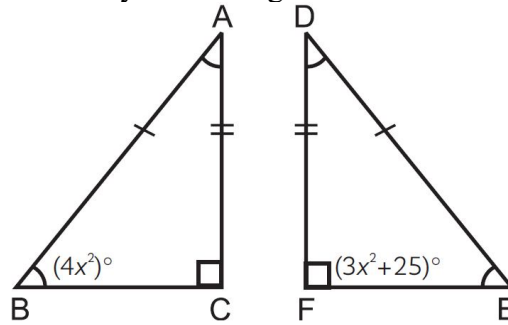
3. If $AB = QR$, $BC = PR$ and $CA = PQ$ in $\triangle ABC$ and $\triangle PQR$, then:
 (a) $\triangle ABC \cong \triangle PQR$ (b) $\triangle CBA \cong \triangle PRQ$ (c) $\triangle BAC \cong \triangle RPQ$ (d) $\triangle BCA \cong \triangle PQR$

4. Consider the triangles shown in the figure. Which of these is not true about the given triangles?



- (a) $\triangle XYZ \cong \triangle STU$ (by SSS congruence rule)
- (b) $\triangle XYZ \cong \triangle STU$ (by RHS congruence rule)
- (c) $\triangle XYZ \cong \triangle STU$ (by ASA congruence rule)
- (d) $\triangle XYZ \cong \triangle STU$ (by SAS congruence rule)

5. If $\triangle ABC \cong \triangle PQR$ and $\triangle ABC$ is not congruent to $\triangle RPQ$, then which of the following is not true?
 (a) $BC = PQ$ (b) $AC = PR$ (c) $QR = BC$ (d) $AB = PQ$
6. $\triangle LMN$ is an isosceles triangle such the $LM = LN$ and $\angle N = 65^\circ$. The value of $\angle L$ is:
 (a) $\angle L = 55^\circ$ (b) $\angle L = 45^\circ$ (c) $\angle L = 50^\circ$ (d) $\angle L = 65^\circ$
7. Ritish wants to prove that $\triangle FGH \cong \triangle JKL$ using SAS rule. He knows that $FG = JK$ and $FH = JL$. What additional piece of information does he need?
 (a) $\angle F = \angle J$ (b) $\angle H = \angle L$ (c) $\angle G = \angle K$ (d) $\angle F = \angle G$
8. In the given figure $\triangle ABC \cong \triangle DEF$ by AAA congruence rule. The value of $\angle x$ is:



- (a) 75° (b) 105° (c) 125° (d) 5°

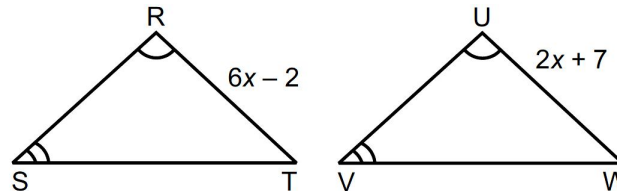
In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.

- (a) Both A and R are true and R is the correct explanation of A.
 (b) Both A and R are true but R is not the correct explanation of A.
 (c) A is true but R is false.
 (d) A is false but R is true.
9. **Assertion (A):** In $\triangle ABC$ and $\triangle PQR$, $AB = PQ$, $AC = PR$ and $\angle BAC = \angle QPR$, $\triangle ABC \cong \triangle PQR$.
Reason (R): Both the triangles are congruent by SSS congruence.
10. **Assertion (A):** Each angle of an equilateral triangle is 60° .
Reason (R): Angles opposite to equal sides of a triangle are equal.

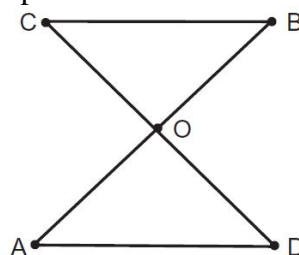
SECTION – B

Questions 11 to 14 carry 2 marks each.

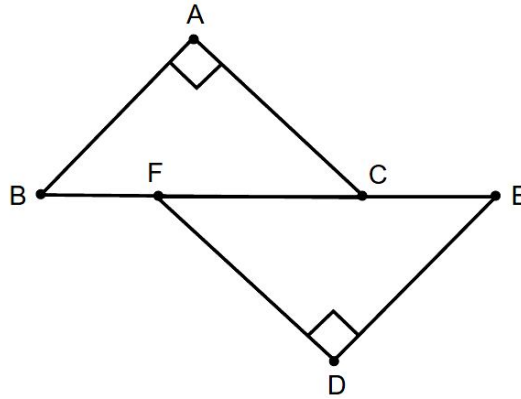
11. In $\triangle RST$, $RT = 6x - 2$. In $\triangle UVW$, $UW = 2x + 7$, $\angle R = \angle U$, and $\angle S = \angle V$. What must be the value of x in order to prove that $\triangle RST \cong \triangle UVW$?



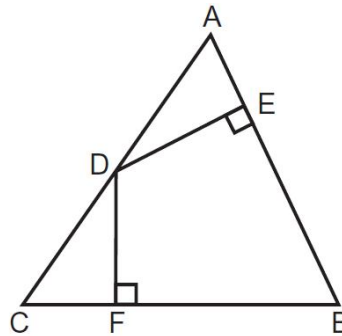
12. In the given figure two lines AB and CD intersect each other at the point O such that $BC \parallel AD$ and $BC = DA$. Show that O is the midpoint of both the line-segment AB and CD.



13. In figure $BA \perp AC$, $DE \perp DF$. Such that $BA = DE$ and $BF = EC$. Show that $\triangle ABC \cong \triangle DEF$.



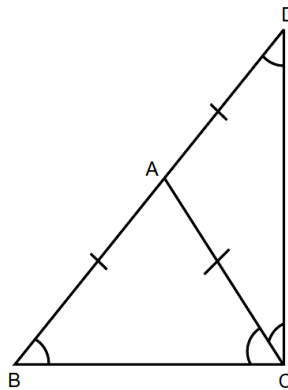
14. In $\triangle ABC$, D is a point on side AC such that $DE = DF$ and $AD = CD$ and $DE \perp AB$ at E and $DF \perp CB$ at F, then prove that $AB = BC$.



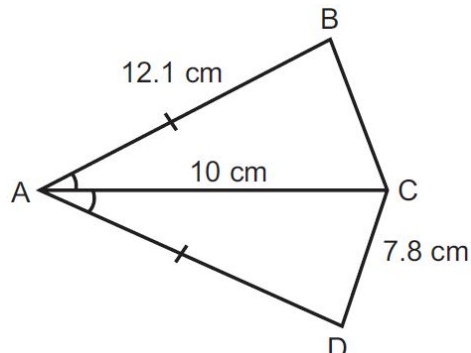
SECTION – C

Questions 15 to 17 carry 3 marks each.

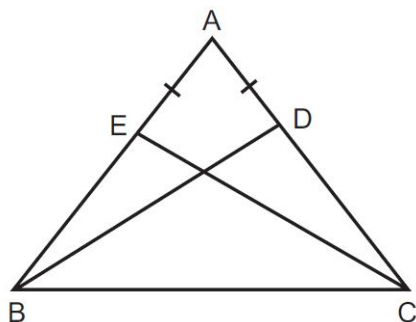
15. $\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$. Show that $\angle BCD$ is a right angle.



16. Find the perimeter of the quadrilateral ABCD (as shown in the figure), if $\angle CAB = \angle CAD$ and also $AB = AD$.



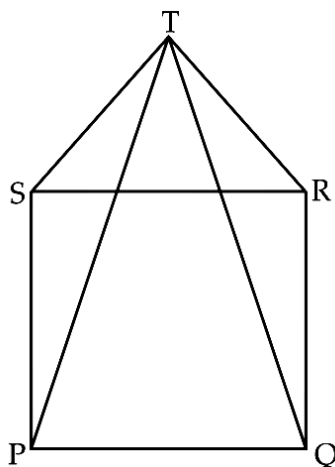
17. ABC is an isosceles triangle with $AB = AC$ and BD and CE are its two medians. Show that $BD = CE$.



SECTION – D

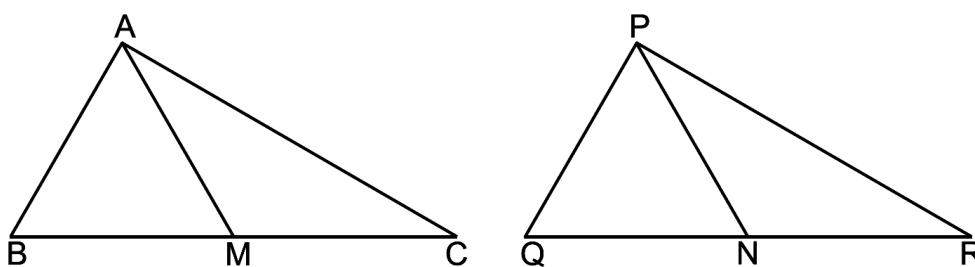
Questions 18 carry 5 marks.

18. In figure, PQRS is a square and SRT is an equilateral triangle. Prove that:
(i) $PT = QT$ (ii) $\angle TQR = 15^\circ$



OR

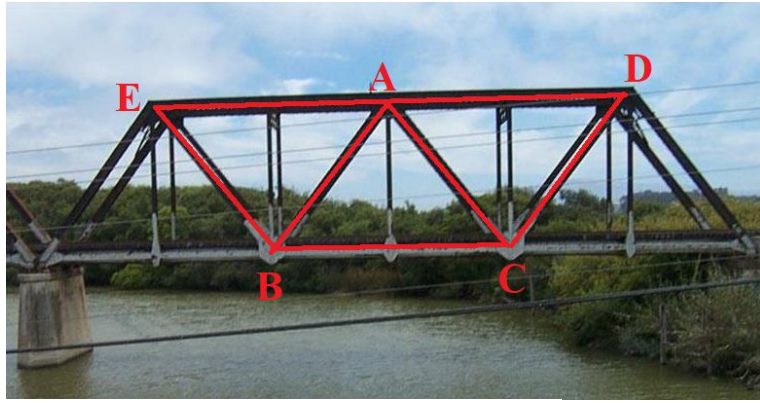
In the below figure, two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of $\triangle PQR$. Show that $\triangle ABC \cong \triangle PQR$.



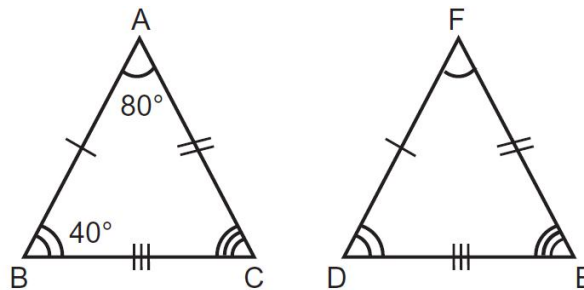
SECTION – E (Case Study Based Questions)

Questions 19 to 20 carry 4 marks each.

19. Truss bridges are formed with a structure of connected elements that form triangular structures to make up the bridge. Trusses are the triangles that connect to the top and bottom cord and two end posts. You can see that there are some triangular shapes are shown in the picture given alongside and these are represented as $\triangle ABC$, $\triangle CAD$, and $\triangle BEA$.



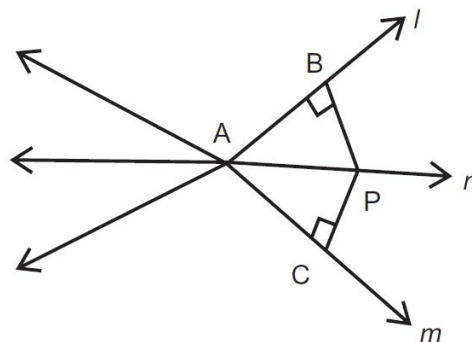
- (a) If $AB = CD$ and $AD = CB$, then prove $\triangle ABC \cong \triangle CDA$ (1)
 (b) If $AB = 7.5$ m, $AC = 4.5$ m and $BC = 5$ m. Find the perimeter of $\triangle ACD$, if $\triangle ABC \cong \triangle CDA$ by SSS congruence rule. (1)
 (c) If $\triangle ABC \cong \triangle FDE$, $AB = 5$ cm, $\angle B = 40^\circ$ and $\angle A = 80^\circ$. Then find the length of DF and $\angle E$. (2)



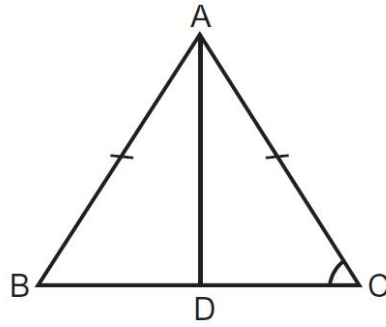
20. To check the understanding of the students of the class about IX the triangles, the Mathematics teacher write some questions on the blackboard and ask the students to read them carefully and answer the following question.



- (a) In figure, P is a point equidistant from the lines l and m intersecting at point A, then find $\angle BAP$. (2)



- (b) In $\triangle ABC$, if $AB = AC$ and $BD = DC$ (see figure), then find $\angle ADC$. (2)



OR

(b) $\triangle LMN$ is an isosceles triangle, where $LM = LN$ and LO , is an angle bisector of $\angle MLN$, Prove that point 'O' is the mid-point of side MN .

