PRACTICE PAPER 09 (2024-25)
CHAPTER 08 INTRODUCTION TO TRIGONOMETRY

SUBJECT: MATHEMATICS **MAX. MARKS : 40**

CLASS : X **DURATION : 1½ hrs**

General Instructions:

(i). **All** questions are compulsory.

(ii). This question paper contains 2**0** questions divided into five Sections A, B, C, D and E.

(iii). **Section A** comprises of **10 MCQs** of **1 mark** each. **Section B** comprises of 4 questions of **2 marks** each. **Section C** comprises of 3 questions of **3 marks** each. **Section D** comprises of 1 question of **5 marks** each and **Section E** comprises of 2 Case Study Based Questions of **4 marks** each.

(iv). There is no overall choice.

(v). Use of Calculators is not permitted

SECTION – A

Questions 1 to 10 carry 1 mark each.

1. $(\sec^2\theta - 1)(\text{cosec}^2\theta - 1)$ is equal to:

(a) –1 (b) 1 (c) 0 (d) 2

2. In Δ ABC right angled at B, $\sin A = \frac{7}{25}$, then the value of cos C is ……

(a) $\frac{7}{25}$ (b) $\frac{24}{25}$ (c) $\frac{7}{24}$ (d) $\frac{24}{7}$

3. If $5\tan\theta = 4$, then the value of $\frac{5\sin\theta - 3\cos\theta}{5\sin\theta + 2\cos\theta}$ is

(a) 1/6 (b) 1/7 (c) 1/4 (d) 1/5

4. If $\text{cosec } A = 13/12$, then the value of $\frac{2\sin A - 3\cos A}{4\sin A - 9\cos A}$

(a) 4 (b) 5 (c) 6 (d) 3

5. Given that $\sin\alpha = 1/2$ and $\cos\beta = 1/2$, then the value of $(\beta - \alpha)$ is

(a) 0° (b) 30° (c) 60° (d) 90°

6. If $\tan\theta = 1$, then the value of $\sec\theta + \text{cosec}\,\theta$ is:

(a) $3\sqrt{2}$ (b) $4\sqrt{2}$ (c) $2\sqrt{2}$ (d) $\sqrt{2}$

7. If $\sin 2A = \frac{1}{2}\tan^2 45°$ where A is an acute angle, then the value of A is

(a) 60° (b) 45° (c) 30° (d) 15°

8. If θ is an acute angle and $\tan\theta + \cot\theta = 2$, then the value of $\sin^3\theta + \cos^3\theta$ is

(a) 1 (b) $\frac{1}{2}$ (c) $\frac{\sqrt{2}}{2}$ (d) $\sqrt{2}$

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

(a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).

(b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).

(c) Assertion (A) is true but reason (R) is false.

(d) Assertion (A) is false but reason (R) is true.

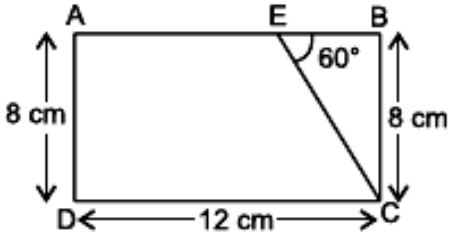
9. **Assertion (A):** In a right ΔABC, right angled at B, if tan A = 1, then 2 sin A. cos A = 1.
Reason (R): tan 45° = 1 and sin 45° = cos 45° = $1/\sqrt{2}$

10. **Assertion (A):** sin (A + B) = sin A + sin B
Reason (R): For any value of θ, $1 + \tan^2\theta = \sec^2\theta$

SECTION – B

Questions 11 to 14 carry 2 marks each.

11. In the given figure, ABCD is a rectangle with AD = 8 cm and CD = 12 cm. Line segment CE is drawn, making an angle of 60° with AB, intersecting AB at E. Find the length of CE and BE.



12. If sin (A + B) = $\sqrt{3}/2$ and sin (A – B) = $\frac{1}{2}$, $0 \le A + B \le 90°$ and A > B, then find A and B.

13. Evaluate: $3\cos^2 60° \sec^2 30° - 2\sin^2 30° \tan^2 60°$.

14. Simplify: $\frac{\tan^2\theta}{1+\tan^2\theta} + \frac{\cot^2\theta}{1+\cot^2\theta}$

OR

If $7\sin^2 A + 3\cos^2 A = 4$, then find tan A

SECTION – C

Questions 15 to 17 carry 3 marks each.

15. If cosecθ + cotθ = p, then prove that $\cos\theta = \frac{p^2-1}{p^2+1}$

16. Prove that $\frac{\sin\theta - \cos\theta + 1}{\sin\theta + \cos\theta - 1} = \sec\theta + \tan\theta$

OR

If sin θ + cos θ = $\sqrt{3}$, then prove that tan θ + cot θ = 1.

17. Prove that: $\frac{\cos^2\theta}{1-\tan\theta} + \frac{\sin^2\theta}{1-\cot\theta} = 1 + \sin\theta\cos\theta$

OR

If cos θ + sin θ = $\sqrt{2}$ cos θ, show that cos θ – sin θ = $\sqrt{2}$ sin θ.

SECTION – D

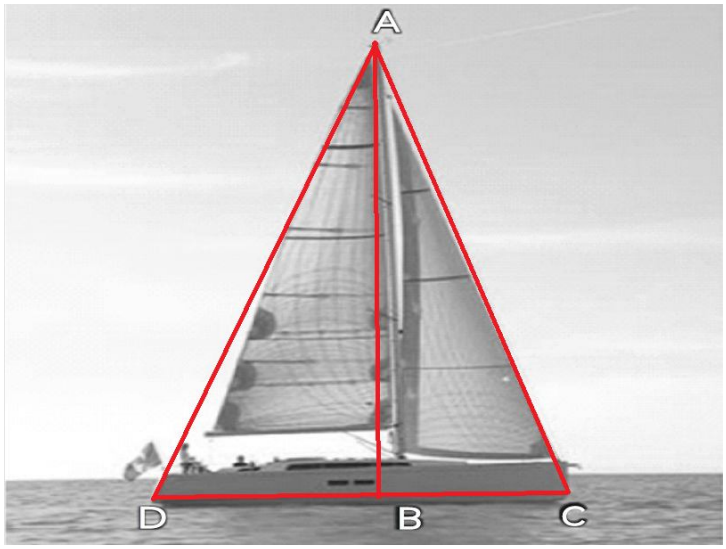
Questions 18 carry 5 marks.

18. (a) Prove that $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$ [3]
(b) If $x\sin^3\theta + y\cos^3\theta = \sin\theta\cos\theta$ and $x\sin\theta = y\sin\theta$ then find $x^2 + y^2$. [2]

SECTION – E (Case Study Based Questions)

Questions 19 to 20 carry 4 marks each.

19. A sailing boat with triangular masts is shown below. Two right triangles can be observed. Triangles ABC and ABD, both right-angled at B. The distance BC = 1 m and BD = 2 m and height AB = 4 m.



Based on the given in formation, answer the following questions:

(a) Find the value of sec D. [1]

(b) Find the value of cosec C. [1]

(c) Find the value of tan D + cot C. [1]

(d) Find the value of $\sin^2 C + \cos^2 D$ [1]

20. Varanasi is a city of temples, including the gold-plated Vishwanath temple of Lord Shiva; the Bharat Mata, or Mother India, temple that boasts a huge three dimensional relief map of the Indian subcontinent carved out of marble; and the hundreds of small temples that dot the waterways and alleys. It is a city of scholars, home to one of Asia's largest universities. It is also a city of legends. The figure below shows one such temple along the banks of the sacred river "Ganges" or "Ganga". A person sitting at point marked A looks at the top of a nearby temple and imagines that a right angled triangle ABC can be drawn as shown in the figure below.

Based on the above information, answer the following questions. (Take $\sqrt{3} = 1.732$)

(a) Find the value of sin A. [1]

(b) Find the value of sin C. [1]

(c) Find the value of tan A – cot C. [1]

(d) Find the value of $\text{cosec}^2 C$. [1]